IEEE Information Theory Society Newsletter



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Obituary for William Lucas Root, 1919-2007

Fred Beutler and Stuart Schwartz

With great sadness we report the death of our friend and colleague, Bill Root, at the age of 87. As an early pioneer in Statistical Communication and Information Theory, Bill transformed the very landscape of the then nascent discipline.

To fully appreciate the impact of Bill Root's early work on statistical communication theory, we need to understand the state of the discipline in the early 1950s. There was no organized curriculum in the area, and the then limited research was carried out by electrical engineers, physicists and mathematicians who were self-taught. Consequently, the theoretical literature consisted of assertions or "theorems" that were vaguely stated, based on unspecified hypotheses, and

"proved" by plausibility arguments. Most researchers were oblivious to such tools we now consider standard: probability measures and structures, ergodicity properties, integration theory (e.g. convergence modes and Fubini's theorem), functional analysis (e.g., Hilbert and Banach spaces), properly applied central limit theorems, spectral representations, etc.

Bill Root was instrumental in placing statistical communication theory on a sound mathematical basis. Two publications were especially influential. The first, affectionately known as "Davenport and Root," is a text introducing seniors and beginning graduate students to the analytical basis of the analysis of signals and systems in the presence of noise. Published in 1958, it was enthusiastically adopted everywhere, and was accepted as the standard text for approximately the next twenty years. Because it introduced most students to this area, the text had tremendous influence in determining the cultural setting of the discipline.

The book provides the student with a sound background in probability theory as a basis of the statistical analysis of signals and systems. Although the mathematical sophistication is consistent with its intended audience, the rigor and accuracy of its approach far exceeded previously existing teaching materials.

The second publication setting the standard for an understanding of the mathematical basis of parameter estimation and detection of signals in noise is another classic, namely the epochal paper generally referred to as "Kelly, Reed and Root,"



which appeared in 1960. An interesting fact illustrating the state of the discipline at that time is that it was rejected by the *IEEE Transactions on Information Theory* as being "too mathematical." Although the methodology and standard of rigor of this work have been well established since, they were innovative and standard setting in their time.

The first part³ applies likelihood testing to various models of a radar signal in gaussian noise with an absolute continuous spectrum. The interest here lies in the use of the Karhunen-Loeve expansion to represent the noise as a convergent in mean sum of mutually independent random variables. The idea, which was novel at the time, was presented

in a rigorous fashion that was far beyond the customary fashion.

The continuation⁴ employs similar methodology to discuss the maximum likelihood estimates of signal parameters, again using statistical decision theory in conjunction with Karhunen-Loeve like expansions. Some special cases are considered, and the structure of the solutions elucidated. As in the first part, the emphasis is on analytical results attained through rigorous mathematical techniques.

His interest in signal detection and information extraction continued with research on applying game theory to develop maximin receivers (1961), studying singular Gaussian measures (1963) and stability issues in detection problems (1964). He continued his collaboration with E. Kelly investigating the sensitivity of radiometric measurements (1963). Later (1968), he developed channel capacity formulas and coding for Gaussian and nonprobabilistic channels. In 1976, he began research on characterizing complex systems in input-output terms, involving abstract spaces and developing function-analytic tools for this purpose. All these investigations involved important problems that were resolved with the precision and rigor that characterized his research and teaching throughout his career.

William Lucas Root was born in Iowa in 1919. In 1940, he graduated from Iowa State University with distinction as a top student in Electrical Engineering. He then went on to

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From the Editor

Daniela Tuninetti

Dear IT society members,

We sadly mark here the passing of Bill Root (1986 Shannon Lecturer), who for so many years played a central role in the IT Society. Our sincere condolences to his family and friends. He will be sorely missed.

I would like to join our president Bixio Rimoldi in congratulating the organizers of ISIT 2007 in Nice, France. The symposium was a great success for the quality of the presentations, the high attendance and the great summer location, the French Riviera. Congratulations to Marc and Giuseppe, and everyone in the great team they put together, for the excellent work. In the next issue you will read several reports about the major ISIT events.

In the meanwhile, in this issue, you will read a detailed summary of Prof. Rudolf Ahlswede's 2006 Shannon Lecture at ISIT in Seattle. You will also find our *regular* columns by our president Bixio Rimoldi, our historian Anthony Ephremides, our creative puzzle maker Sol Golomb, and NSF program manager Sirin Tekinay.

In addition we also have a report by Marc Fossorier about the different society awards

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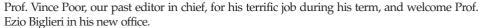
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announced at ISIT 2007, the minutes of the Board of Governors meeting in Baltimore by Joao Barros, the call for nominations for the Debrushin Award and the IEEE New Initiatives call. At the end of this issue you will find some new calls for papers.

Last but not the least, Prof. Ezio Bigleri, the new editor in chief of the Information Theory Transactions, contributed to this issue with an editorial that outlines some of the initiatives for the term he started to serve at the end of June. I profit of this occasion to thank



Let me conclude with a couple of notes. I am delighted that the Board of Governors in Nice approved my request to increase the newsletter budget so as to support an html online version for the new society website. From 2008, for a trial period of one year, IEEE will produce both a pdf and an html version of the newsletter. I urge everyone to provide feedback on this initiative as your opinion will be crucial to renew the funding for this now on-line service. And this brings me to the second note. You can provide you feedback and comments to the newsletter authors and editor by sending your letters to me (see my email contact information below.) I will try to answer them in the *Letters to the Editor* column that I inaugurate in this issue. Please profit of this exclusively reserved space to make the newsletter a space "closer" to the need and expectations, and expressing the opinion of, the society members. Thanks in adavance.

At the time I wrote this column in early July, my piece would end here -- with a reminder of the deadlines for the incoming issues of the newsletter and my contact information. By the time I was reviewing the proofs of this issue in late July, I was informed of the tragic passing away of Prof. Sergio Servetto. Sergio, assistant professor in Cornell, was an ardent scholar, an active member of our society, and a dear friend of mine. I first met Sergio in 2002 at ISIT. From that

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MIT, where he earned the master's degree in Electrical Engineering in 1943. His further education was interrupted by World War II; he served as a Marine officer until the end of the war. Returning to MIT, he earned the doctorate in mathematics in 1952.

Upon receiving his doctorate, Bill joined the Analysis Group at Lincoln Laboratories, becoming its head in the period 1959-1961. It was during his stay at Lincoln Laboratory that Bill first became involved in the statistical analysis of radar signals.

In 1962, and until his retirement in 1987, Bill was Professor of Aerospace Engineering at the University of Michigan. However, his reputation as a leading researcher brought him many invitations to teach and do research elsewhere; he served in Visiting Professor capacity at the University of California at Berkeley and Michigan State University, and as a Visiting Scholar at Cambridge University and the Mathematics Research Center at the University of Wisconsin.

In recognition of his research, Bill was made a Fellow of the IEEE in 1965. He was further recognized as a National Science Foundation Senior Postdoctoral Fellow (1970). In 1986, as Shannon Lecturer, he received the highest honor bestowed by the *IEEE Professional Group on Information Theory*; at the time, he was cited for "...consistent and profound contributions to the field of information theory."⁵

Bill Root was widely admired by his colleagues, not only for research prowess, but for his sterling personal qualities. He combined a dry wit with an unusually modest and humble demeanor. His integrity was legendary; he refused to present results that were not rigorously stated and proved. On at least one occasion, he withdrew a paper that had already been accepted, on the grounds

that he felt that the results therein were not sufficiently important.

As a research advisor for doctoral students, he motivated his doctoral students to meet his high standards and continually extend their horizons. As a classroom teacher, he was simply superb—direct and clear, demanding yet at an appropriate student level. Many of his classroom students volunteered that he was the "best teacher they ever had."

Professor Root was the organizer and first chairman of the graduate program in computer, information, and control engineering at the Univeristy of Michigan, which for many years was renowned for the distinction of its faculty and students. He treated colleagues and students alike, demanding from them integrity, high standards, precision in research, and a little bit of humility. He did this with his easy manner and good humor.

Bill will be missed by all those who had the good fortune to interact with him.

- ¹ W. Davenport and W.L. Root, An Introduction to the Theory of Random Signals and Noise, McGraw-Hill, New York (1958)
- ² Personal communication by William L. Root
- ³ K.J. Kelly, L.S. Reed, W.L. Root, The detection of radar echoes in noise I. J. Soc. Indus. Appl. Math., 8, 309-341 (1960)
- ⁴ K.J. Kelly, L.S. Reed, W.L. Root, The detection of radar echoes in noise II. J. Soc. Indus. Appl. Math., 8, 481-507 (1960)
- ⁵ Personal communication by William L. Root

From the Editor continued from page 2

very first meeting, I was touched by his warm personality, sense of humor, and enthusiasm for research. Our passion for information theory made as become friends. Over the years, Sergio became a family friend because of his love for flying that he shared with by my finance Chris. Chris and I were shocked and deeply sadden by the news of the plane crash that killed him. We had only just talked during ISIT in Nice with Sergio and we were looking forward to welcome him and his family in Chicago, so close to Notre Dame. I miss Sergio's enthusiasm, good spirts and boundless energy. My my deepest condolences to his wife Viviana, his sons Alejandro and Luciano, and all his friends.

Please help to make the Newsletter as interesting and informative as possible by offering suggestions and contributing news. The deadlines for the next few issues of the Newsletter are as follows (please notice that the deadlines have been moved forward by about a week with respect to the past):

 Issue
 Deadline

 December 2007
 October 10, 2007

 March 2008
 January 10, 2008

 June 2008
 April 10, 2008

 September 2008
 July 10, 2008

Electronic submission in Ascii, LaTeX and Word formats is encouraged. Potential authors should not worry about layout and fonts of their contributions. Our IEEE professionals take care of formatting the source files according to the IEEE Newsletter style. Electronic photos and graphs should be in high resolution and sent in as separate file.

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I wish everyone a great beginning of the fall semester.

Daniela Tuninetti

President's Column

Bixio Rimoldi



I am writing this column upon my return from ISIT in Nice, France. What an appropriate name for such a great conference (and what a fitting logo). The organization was great. Once again I would like to thank the organizers (too many to mention) and in particular the conference co-chairs Giuseppe Caire and Marc Fossorier, and the co-chairs of the technical program committee, namely Andrea Goldsmith, Muriel Medard, Amin Shokrollahi and Ram Zamir. Special thanks

also go to Ms. Stefania Albis and her staff for taking care of logistics in a professional and friendly manner.

Each ISIT is preceded by a Board of Governors (BoG) meeting. In this issue I am focusing on last meeting's highlights. They are:

- (1) The Online Committee has been charged to come up with the specs of a new forward-looking multi-purpose web site. Anybody who is interested in helping should contact the chair of the Online Committee, Nick Laneman. The plan is to have a project presented at the next BoG meeting in September.
- (2) The Society has charged the Student Committee with the organization of a Winter or Summer School on Information Theory and Coding. Suggestions should go to Andrea Goldsmith.
- (3) Ezio Biglieri, incoming Editor in Chief of the IT Transactions, has raised a number of important questions. Some of these and other questions raised in the subsequent discussion are:

 (a) Given the difficulty of finding expert and responsive reviewers and given the opportunity offered by the fact that some papers that are in the review process are also available through arXiv, should the Society permit/encourage the readers of such papers to send comments to the Editor in Chief?;

 (b) Is it still desirable to have two categories of papers (Regular Papers and Correspondence Items)? (c) Should the IT Transactions consider a short paper which is the identical

copy of a paper submitted to an ISIT or to an ITW? After all, conferences and journals fulfill different needs. ISITs and ITWs offer interaction and timeliness whereas the Transactions offer the highest level of quality control. Both are needed; (d) Should the society encourage more tutorial and/or state-of-the-art papers?; (e) Should we create a Magazine devoted to society news (like our current Newsletter) and to light tutorial papers? (A good example of this is the Signal Processing Magazine.) The BoG has approved the appointment of an ad-hoc committee that will consider these and possibly other publication questions. Inputs should be sent to Ezio Biglieri.

- (4) The BoG approved a motion stating that conference papers not presented by an author be withdrawn from IEEE Xplore.
- (5) During a one-year trial period there will be an HTML version of the Newsletter.
- (6) An ad-hoc committee on New Initiatives was approved. For the time being, ideas concerning new initiatives should be submitted to the Second Vice President, Andrea Goldsmith.
- (7) The awards that needed BoG approval were finalized. To know the name of the winners, please refer to the "Award Announcement" article later in this issue. All new awards were announced at the banquet.

The next and last BoG meeting of 2007 will be held on September 27 at Allerton, Monticello, IL. It will be an important meeting since the BoG will have to decide whether or not to go ahead with a number of initiatives, chief among them is the web re-design. As always, the meetings are open to everyone.

In the meanwhile we have received the reports of the quinquennial IEEE review of the IT Society. The Society Review report is rather positive and the Publication Review report is glowing. I will give more detailed comments in my next and last President's Column.

The Historian's Column

Anthony Ephremides

In the past I have mused frequently over our society's relationship with its soviet counterpart during the Cold War era. Prompted by the recent workshop in Chengdu, China, I would like to review our relationship with the Chinese. It has been a very different, much less turbulent, and, perhaps, much more consequential than our dealings with the Soviets.

When Information Theory was born, China was in serious political, economic, and military internal turmoil. It was heuristically closed to most of the rest of the world and there were hardly any communication with the country's scientists. Especially during the dire cultural Revolution period any thoughts about entropy and error correction might result in hard labor in the fields for the purpose of personal fault correction.

But then Nixon went to China (even an opera has been written to dramatize that historic visit), Mao passed away, the power struggle that ensued was more or less resolved, and, lo-and-behold, in 1979 at the ISIT in Grignano, Italy, two Chinese professors showed up. It is still unclear by whom and when Shannon's paper was first read in China. The fact is that by 1979 there had been a sufficient amount of knowledge and interest generated in that vast country. There were discussions between the Chinese delegates and many of our members. The most productive discussion seems to have taken place with Dick Blahut and Toby Berger. They were both invited to visit China and lecture on Information Theory for several weeks.

I recall a telegram that had been received in 1981 by the society's president who proceeded to read it to the members of the Board of Governors during a BoG Meeting. It was an enthusiastic account of their experience and it recommended a definite cultivation of contacts with the Chinese. The reaction and level of interest that their lectures generated had apparently exceeded their expectations.

The next thing that happened was the arrival of two Chinese students at Cornell University who had been encouraged to apply for admission to the Ph.D. Program. They were to study under Toby Berger and they were destined to be the pioneers of a long, sustained, and expanded procession of additional students from China who joined colleagues from Hong Kong and Taiwan in populating American and European Universities. One of them was our very familiar Zhen Zhang who has been with the faculty of the University of Southern California since 1988.

The rest is ... well, history. Very quickly, at the same staggering pace with which the entire country and its Society has been profoundly transformed, Information Theory grew into the mainstream of scientific activity in China. There was already a workshop in the outskirts of Beijing (in the Fragremt Hill's Hotel) in 1988 right after the Kobe ISIT in Japan. I still remember an early morning hike to the surrounding hills with Bruce Hajek and Tom Cover leading the way amidst many Chinese hikers who were periodically emitting loud yells and cries of greeting and relaxation.

Another workshop was planned to take place in 2003 in Hong Kong

(by then already an integral part of China) following the Yokohama ISIT in Japan. Alas, fears arising from the "bird flu" epidemic that broke out early that year forced the cancellation of that workshop for which Raymond Young (among others) had labored so intensely.



Despite that setback, through the sustained efforts of people like Raymond Yeung, Shu Lin, Ping Li, and others, the very successful recent workshop in Chengdu took place finally last Fall. This workshop revealed the depth and breadth of the "hold" that Information Theory has created in China. The majority of the participants were from China and they displayed talent, enthusiasm, and creativity. Dick Blahut reminisced about the sequence of events that culminated in the current healthy growth of Information Theory in China (and by Chinese researchers worldwide). He likened the initiative of Shu Lin's (who had actually instigated the original visit and participation by Chinese delegates in the 1979 ISIT) to the planting of an acorn, that usually grows into a towering and robust oak tree. During the workshop banquet, where Dick made these remarks, we were treated to fantastic performances by diverse artists and, of course, sumptuous Chinese food, washed down with, among other libations, Great Wall Cabernet Sauvignon.

I cannot refrain from adding a personal note that shows how small our vast world sometimes is. Being interested in opera and operatic singing I noted during the banquet performance a young soprano (whose name is Emma) who interpreted some Chinese songs with a bright clarion voice. As it happens there is also an exciting new discovery of a great tenor in the international opera scene, called Yu Qiang Dai. He has only made one recording in the West (consisting of Halian opera arias that he interprets with unbelievable Italienate sound and faultless Italian diction) and he has sung in Tosca at Covent Garden in 2005. He is young and talented and belongs to the pantheon of tenors along with Caruso, DelMonaco, Corelli, Domingo, Pavarotti, and others. So, I thought that in China I might find more recordings by him. I approached Emma during the banquet and asked her whether she knew of this great new tenor. After asking me to spell his name and reflecting, she concluded she didn't. But, about fifteen minutes later she can back with a beaming face. She had talked to her husband, who is an Information Theorist and who clarified to her that indeed Qiang Dai Yu (notice the reversal in the sequence of the names) was a colleague of her uncle with whom he had studied music together. In a country of 1.2 billion people I had located a "distance-one" neighbor of Yu Qiang Dai in such an effortless way! Emma brought me the next day additional recordings that he has made in China and she even e-mailed me additional performances by him recently, what a beautiful side-event that matched fittingly this wonderful workshop! Unlike the country's historic "long march" under Mao, its march into Information Theory has been swift and very successful.

Shannon Lecture at ISIT in Seattle 13th July 2006: Towards a General Theory of Information Transfer

R. Ahlswede, Faculty of Mathematics, University of Bielefeld, Bielefeld, Germany http://www.math.uni-bieleteld.de/ahlswede/it.html



"More than restoring strings of symbols transmitted means transfer today."

Introduction

We all know that C.E. Shannon in his paper [97] presented a theory of Transmission over Noisy Channels based on the concept of codes. He considered crucial performance criteria like rates and error probabilities, predicted there connections and outlined proofs for them. (For a unification in terminology we refer to [11]). Subsequently he was involved in refining estimates and in inspiring others to do so. As highlights we point at the two papers [100] and [101]. Another aspect, complexity of coding, gave a strong impetus to several theoretical and practical inventions of concepts and methods, which kept a large community of scientists busy for more than fifty years now. It is not our aim to describe or comment on these developments. That has been done in many books and articles. Recently two of them, [56] and [71], came in our hands and we can recommend them. A similar situation can be encountered in Data Compression—lossless and lossy meeting fidelity criteria—Shannon's other favorite research area within Information Theory. Also here most optimality results (Source Coding Theorems) are—very similar to the situation in Statistics—of an asymptotic nature. A reminder for going to more practicability came from Ziv's lecture [117].

After these preliminary remarks we come to start to justify our (ambitious) title. Perhaps the most direct and easy way is to draw attention to two statements of Shannon from his paper [97] concerning communication and filtering (also called denoising), respectively.

"The fundamental problem of communication is that of reproducing at one point either exactly or approximately a message selected at another point."

"If the source already has a certain redundancy and no attempt is made to eliminate it ... a sizable fraction of the letters can be received incorrectly and still reconstructed by the context."

Both times the goal of reproducing transmitted data is clearly expressed.

However transmission is not the only goal of communication for

human beings (and animals?!). A step beyond this goal of Shannon's celebrated theory of communication was made with our creation of a theory of identification in the presence of noise. The mathematical foundations were laid together with G. Dueck and carried on by Verboven, van der Meulen, Zhang, Cai, Csiszár, Han, Verdu, Steinberg, Anantharam, Venkataram, Wei, Csibi, Yeong, Yang, Shamai, Merhav, Burnashev, Bassalygo, Narayan and many others.

To fix ideas, *transmission* (classical) concerns the question "How many messages can we transmit over a noisy channel?" One tries to give an answer to the question "What is the actual message from $\mathcal{M} = \{1, \ldots, M\}$?"

On the other hand in *identification* it is asked "How many possible messages can the receiver of a noisy channel identify?" One tries to give an answer to the question "Is the actual message i?" Here i can be any member of the set of possible messages $\mathcal{N} = \{1, 2, \dots, N\}$.

This theory initiated other research areas like Common Randomness, Authentication in Cryptology, Alarm Systems. It also led to the discovery of new methods which become fruitful also for the classical theory of transmission, for instance in studies of robustness like arbitrarily varying channels, optimal coding procedures in case of complete feedback, novel approximation problems for output statistics and generation of common randomness, the key issue in Cryptology.

Moreover our work on identification has led us to reconsider the basic assumptions of Shannon's Theory. It deals with "messages", which are elements of a *prescribed set of objects*, known to the communicators. The receiver wants to know the true message. It has been emphasized with the two citations from Shannon 1948 above! However, this basic model occurring in all engineering work on communication channels and networks addresses a very special communication situation. More generally they are characterized by

- (I) The questions of the receivers concerning the given "ensemble", to be answered by the sender(s)
- (II) The prior knowledge of the receivers
- (III) The senders prior knowledge.

It seems that the whole body of present day Information Theory will undergo serious revisions and some dramatic expansions. A general theory of information transfer abbreviated as GTIT, was developed and to some degree analyzed in [13]. It extends the frontiers of Information Theory in several directions.

The main contributions concern information transfer by channels. There are also new questions and some answers in new models of source coding. While many of our investigations are in an explorative state, there are also hard cores of mathematical theories [13]. In particular we present a unified theory of information transfer, which naturally incorporates Shannon's theory of information transmission and the theory of identification in the presence of noise as extremal cases. It provides several novel coding theorems based on randomized encoding. Quite surprisingly whereas Shannon's coding theorem for transmission shows that sizes of maximal message sets grow exponentially in the block length of optimal codes used for fixed guaranteed error probability, now, for instance already for identification typically there is a double exponentially growth and we determine again the best exponent, called now second order capacities, exactly (see [16], [34], [35], [41], [44], [47], [77], [78], [85], [107]).

On the source coding side we introduced data compression for identification and discovered the identification entropy.

Finally we mention as a new and perhaps most promising direction the study of probabilistic algorithms with identification as *concept of solution* in mathematics. (For example: for any *i*, is there a root of a polynomial in interval *i* or not?)

The algorithm should be fast and have small error probabilities. *Every algorithmic problem* can be thus considered. This goes far beyond Information Theory. Of course, like in general information transfer also here a more general set of questions can be considered. As usual in Complexity Theory one may try to classify problems. What rich treasures do we have in the much wider areas of information transfer?!

A General Communication Model

The goal in the classical Shannon communication theory is to transmit many messages reliably over the channel W. This is done by coding. An (n, M, λ) -code is a system of pairs $\{(u_i, D_i) : 1 \le i \le M\}$ with $u_i \subset \mathcal{X}^n, D_i \subset \mathcal{Y}^n$ and

$$D_i \cap D_{i'} = \emptyset$$
 for $i', i \neq 1, ..., M$,
 $W^n(D_i^c|u_i) \leq \lambda$ for $i = 1, ..., M$.

Given a set of messages $\mathcal{M} = \{1, \ldots, M\}$, by assigning i to codeword u_i we can transmit a message from \mathcal{M} in blocklength n over the channel with a maximal error probability less than λ . Notice that the underlying assumption in this classical transmission problem is that both, sender and receiver, know that the message is from a specified set \mathcal{M} . They also know the code. The receiver's goal is to get to know the message sent.

One can conceive of many situations in which the receiver has (or many receivers have) **different goals**.

A nice class of such situations can, abstractly, be described by a **family** $\Pi(\mathcal{M})$ **of partitions of** \mathcal{M} . Decoder $\pi \in \Pi(\mathcal{M})$ wants to know only which member of the partition $\pi = (A_1, \dots, A_r)$ contains m, the true message, which is known to the encoder.

We describe now some seemingly natural families of partitions.

Model 1: $\Pi_S = \{\pi_{Sh}\}, \pi_{Sh} = \{\{m\} : m \in \mathcal{M}\}.$ This describes Shannon's classical transmission problem stated above.

Model 2: $\Pi_I = \{\pi_m : m \in \mathcal{M}\}$ with $\pi_m = \{\{m\}, \mathcal{M} \setminus \{m\}\}$. Here decoder π_m wants to know whether m occured or not. This is the identification problem.

Model 3: $\Pi_K = \{\pi_S : |S| = K, S \subset \mathcal{M}\}$ with $\pi_S = \{S, \mathcal{M} \setminus S\}$. This is an interesting generalisation of the identification problem. We call it *K*-**identification** (relation to superimposed codes, Kautz/Singleton Codes).

This case also arises in several situations. For instance every person π_S may have a set S of K closest friends and the sender knows that one person $m \in \mathcal{M}$ is sick. All persons π_S want to know whether one of their friends is sick.

Model 4: $\Pi_R = {\pi_r : \pi_r = \{\{1, ..., r\}, \{r+1, ..., M\}\}\}}$. Here decoder π_r wants to know whether the true message exceeds r or not. We speak of the ranking problem.

Model 5: $\Pi_B = \{ \{A, \mathcal{M} \setminus A\} : A \subset \mathcal{M} \}$. Here $\pi_A = \{A, \mathcal{M} \setminus A\}$ wants to know the answer to the binary question "Is m in A?".

Model 6: $\mathcal{M} = \{0, 1\}^{\ell}$, $\Pi_C = \{\pi_t : 1 \le t \le \ell\}$ with $\pi_t = \{\{(x_1, \dots, x_{\ell}) \in \mathcal{M} : x_t = 1\}, \{(x_1, \dots, x_{\ell}) \in \mathcal{M} : x_t = 0\}\}$. Decoder π_t wants to know the t-th component of the vector valued message (x_1, \dots, x_{ℓ}) .

In all these models we can consider the first (or second) order capacities. They are known for models 1, 2. It is shown in [13] that for models 4 and 5 the capacities equal Shannon's transmission capacity.

The most challenging problem is the general K-identification problem of model 3. Here an (n, N, K, λ) -code is a family of pairs $\{(Q(\cdot|i), D_{\pi}): 1 \leq i \leq N, \pi \in \Pi_K\}$, where the $Q(\cdot|i)$'s are PD's on $\mathcal{X}^n, D_{\pi} \subset \mathcal{Y}^n$, and where for all $\pi = \{S, \mathcal{M} \setminus S\}$ $(S \in \binom{\mathcal{M}}{K})$

$$\begin{split} & \sum_{x^n} Q(x^n|i) W^n \left(D_{\pi}^c | x^n \right) \leq \lambda \quad \text{for all} \ \ i \in S, \\ & \sum_{x^n} Q(x^n|i) W^n \left(D_{\pi} | x^n \right) \leq \lambda \quad \text{for all} \ \ i \notin S. \end{split}$$

Example 1 In a certain lottery a player can choose ℓ of the numbers $1, \ldots, L$, say, $\{a_1, \ldots, a_\ell\}$. A set $\{b_1, \ldots, b_\ell\}$ of ℓ numbers is choosen at random.

Suppose that T players have chosen $\{a_1^1,\ldots,a_\ell^1\},\ldots,\{a_1^T,\ldots,a_\ell^T\}$, resp. Every player wants to know whether he won, that shall mean, whether he has at least $\ell-1$ correct numbers: For the t-th player

$$\left|\left\{a_1^t,\ldots,a_\ell^t\right\}\cap\{b_1,\ldots,b_\ell\}\right|\geq \ell-1.$$

How many bits have to be transmitted in a randomized encoding, so that every player **knows with high probability**, **whether he won**.

Example 2 Lets view the elements of $\{1, ..., a\}^n$ as sequences of events. Historians (or observers of stockmarkets) have a subsequence of events, say,

$$\left(t_1^1,\ldots,t_{s_1}^1\right),\ldots,\left(t_1^\ell,\ldots,t_{s_\ell}^\ell\right).$$

The ℓ persons are to be informed with high probability correctly about the correct sequence of events.

Example 3 In some countries 40% of the healthy men of a year are drafted by random selection. Every candidate wants to know with high probability correctly whether he is among them. This falls under model 6.

There are of course several other situations described by a family $\Pi(\mathcal{M})$ of partitions of \mathcal{M} . There are others, which do not fall exactly in this setting. One of them is that of L-identification introduced by Christian Heup in [82] for source coding. For a one-way channel, which we assume to be a discrete memoryless channel, abbreviated as DMC, L-identification refers to the situation where an L-subset of \mathcal{M} is given to the encoder. For example, the encoder knows L persons $m_1, \ldots, m_L \in \mathcal{M}$, who have won a lottery. On the receiver's side, a member of \mathcal{M} , wants to know whether or not he or she is among the winners. However, the information in which a participant is interested can no longer be represented by a partition of \mathcal{M} . We have to partition $\binom{\mathcal{M}}{L}$ and get

$$\Pi_{L,\text{set}} = \{ \pi_m : m \in \mathcal{M} \},$$

where $\pi_m = \{S_m, \binom{\mathcal{M}}{L} \setminus S_m\}$ and $S_m = \{S \in \binom{\mathcal{M}}{L} : m \in S\}$. We call this model *L-identification for sets*.

One could also think of situations where the L objects, which are known to the encoder, need not be pairwise different. We call this L-identification for vectors. The model for this is

$$\Pi_L = \{ \pi_m : m \in \mathcal{M} \},$$

where $\pi_m = \{A_m, \mathcal{M}^L \backslash A_m\}$ and

 $A_m = \{A \in \mathcal{M}^L : A \text{ has at least one component equal to } m\}.$

Encoding and decoding have to be devised so that every partici-

pant, a member of $\ensuremath{\mathcal{M}}$ can make his decision with small probability of error.

The theory of identification led us to the discovery of the concept of common randomness. The interplay between second order identification capacity and first order common randomness capacity is discussed in the Introduction of the book [19] on pages 6–16 and in our Shannon Lecture (http://media.itsoc.org/isit2006/ahlswede/).

For further important work on common randomness we refer to the papers [31], [32], [65], [84], [91], [92], [95], and [112].

Whereas Shannon is usually credited as the founder of Information Theory in a probabilistic setting, Hamming is often mentioned as the originator of combinatorial models for communication.

In our report of results we follow this devision, also comment on combi-probabilistic models, and finally give further perspectives.

It has been reported that Shannon devoted a great part of his lecture at the 1973 ISIT in Ashkelon to feedback. Still it is recorded that in 1998 at a workshop of the Netherlands Academy of Sciences a well-known member of the Information Theory Society articulated his position that feedback problems don't belong to channel coding theory, especially for AVC-channels. In his lecture "Information Theory after Shannon" in Bielefeld, August 12, 2003 Massey mentioned that "Shannon never treated feedback with the same sweeping generality that he did with almost everything else he founded." and added that in his opinion "Shannon was trying to encourage his "followers" to take up this subject." In his 1990 paper [90] he gave his support to Marko's ([89]) concept of directional information for channels with feedback. Those are views, which we share, and this is documented in chapter 2 of [42]

We emphasize that GTIT can also be studied in the presence of feedback.

In the late 70-ties we wrote with I. Wegener the first book on search [42]. Its title "Search Problems" indicates the explorative state of the subject at that time. Contributions (often the same several times) came from Statistics, Economy, Computer Science or even entertainment games. We started viewing the subject as part of Information Theory.

In general a search problem can be formulated as a coding problem for channels with passive noiseless feedback. Furthermore noiseless source coding can be described as a search problem with probabilities on the search space. It is remarkable that very different kinds of problems could be classified as search problems and that researchers from various fields often know little about results achieved in areas in which they don't work.

The significance of the feedback scheme in [2] (see also [3] and [25] for robust versions), which is based on iterative list reductions, has been recognized after many years and the construction has been made the basis of the book [96].

Again there are probabilistic and combinatorial models.

In order to convey the flavor of the later subject to a broader scientific community we present below the solution of a seemingly basic classical problem.

The Rényi-Berlekamp-Ulam **search game with** t **lies** has an equivalent formulation in terms of transmission of messages over a noisy binary channel with t errors in the presence of feedback. For block length n and error fraction $\tau = \frac{t}{n}$ the optimal rate for all large n we call capacity-error function $C_2(\tau)$.

In his 1964 MIT thesis Berlekamp found a coding strategy achieving equality of C_2 with the Hamming bound H_2 for infinitely many τ . He also showed that C_2 coincides with the tangent at H_2 through the point $(\frac{1}{3}, 0)$.

In joint work with C. Deppe and V. Lebedev we discovered a coding scheme which gives such results for all alphabet sizes q. Surprisingly the corresponding tangent at H_q , the q-ary Hamming bound, starts for every $q \ge 3$ at $(\frac{1}{2}, 0)$!

There is a great variety of search problems caused by different error concepts, types of questions, and the structure of objects searched for (the most prominent example being group testing). The flavor can be gained from [66].

A. Probabilistic Models

I Transmission via DMC (Shannon Theory)

How many possible messages can we transmit over a noisy channel? Transmission means there is an answer to the question: "What is the actual message?"

Define $M(n, \lambda) = \max\{M : \exists (n, M, \lambda)\text{-code}\}.$

Shannon 48: $\lim_{n\to\infty} \frac{1}{n} \log M(n,\lambda) = C$, where the capacity $C = \max_X I(X \wedge Y)$ and the mutual information $I(X \wedge Y)$ equals H(X) - H(X|Y), that is, the difference of the entropy H(X) and the conditional entropy H(X|Y).

II Identification via DMC (Including Feedback)

How many possible messages can the receiver of a noisy channel identify? Identification means there is an answer to the question "Is the actual message i?", where i can be any member of the set of possible messages $\{1, 2, ..., N\}$. Here randomisation helps!!!

 $\{(Q(\cdot|i), D_i) : 1 \le i \le N\}$ is an $(n, N, \varepsilon_1, \varepsilon_2)$ ID-code of $Q(\cdot|i) \in \mathcal{P}(\mathcal{X}^n)$ = set of all PD on $\mathcal{X}^n, D_i \subset \mathcal{Y}^n$, and

- (1) $\sum_{x^n \in \mathcal{X}^n} Q(x^n|i) W^n(D_i^c|x^n) \le \varepsilon_1 (1 \le i \le N)$ (Error of 1st kind: i rejected, but present)
- (2) $\sum_{x^n \in \mathcal{X}^n} Q(x^n | j) W^n(D_i | x^n) \le \varepsilon_2 \forall i \ne j$ (Error of 2nd kind: i accepted, but some $j \ne i$ present).

Define $N(n, \varepsilon) = \max\{N : \exists (n, N, \varepsilon, \varepsilon) \text{ ID-code}\}.$

Theorem AD_1 (Double exponent.–Coding Theorem and soft converse)

(1)
$$\lim_{n\to\infty} \frac{1}{n} \log \log N(n, \varepsilon) \ge C \ \forall \varepsilon \in [0, 1]$$

(2)
$$\overline{\lim}_{n\to\infty} \frac{1}{n} \log \log N(n, 2^{-\delta n}) \le C \ \forall \delta > 0.$$

(Han/Verdú
$$\lim_{n\to\infty} \frac{1}{n} \log \log N(n, \varepsilon) = C \ \forall \varepsilon \in (0, \frac{1}{2})$$
)

C = second order identification capacity = Shannon's (first order) transmission capacity.

Theorem AD₂ In case of **feedback** the 2-order ID-capacities are, if C > 0.

without randomisation $C_f(W) = \max_{x \in \mathcal{X}} H(W(\cdot|x))$ and with randomisation $C_f(W) = \max_P H(PW) \ge C$.

Phenomena:

- 1. Feedback increases the optimal rate for identification.
- 2. **Noise** can increase the identification capacity of a DMC in case of feedback (think about probabilistic algorithms, here noise creates the randomisation, which is not the case for Shannon's theory of transmission)
- Idea: Produce a "big" (large entropy) random experiment with a result known to sender and receiver and use the Transformer Lemma below.

"Principle": Entropy of a large common random experiment = ID–capacity of 2-order (region).

Remark ID-theory led to the foundation of new areas and stimulated further research.

Approximation of output distributions

It originated from converse proofs in Theorem AD₁. How can we count? For $P \in \mathcal{P}(\mathcal{X}^n)$ find minimal $\mathcal{U} \subset \mathcal{X}^n$ with uniform distribution $P_{\mathcal{U}}$ such that $P_{\mathcal{U}}$ $W \sim PW$. Then $N \lesssim \binom{|\mathcal{X}^n|}{|\mathcal{U}|}$.

Information measures

How do we measure information, by the Cn bits in Shannon's fundamental theorem or by the $\log Cn$ bits in our Theory of Identification?

<u>Common Randomness Capacity</u>

It was observed in [35] that in Identification the second order rate is essentially determined by the first order rate of a random experiment set up by the communicators and whose outcome is known to both, sender and receiver, with high probability. In other words instead of the requirement for the receiver to recover the message sent by the sender with high probability it is required for the communicators to know the value of the same random variable with high probability. Thus a new concept, different from

both, transmission and identification, but with interesting connections to them was introduced. It is now called **common randomness**. A systematic presentation can be found in [31], [32]. Many interesting and important results and applications of common randomness have been obtained so far. When we speak of GTIT today we mean it to include at its core the theory of information transmission, common randomness, identification and its generalizations and applications, but it goes far beyond it even outside communication theory when we think about probabilistic algorithms with identification (or more general tasks) as concepts of solution!

Actually, the origin of the concepts **common randomness and common randomness capacity** took a fascinating path. Immediately after [34] the results of [35] were discovered—the papers appeared face by face in the same volume. An output process Y_1, \ldots, Y_n produced by a DMC from an input process X_1, \ldots, X_n is not only known to the receiver of the channel W, but also to its sender, if there is a noiseless (passive) feedback channel. This common knowledge of the random process was used in [35] for the randomization in a randomized identification procedure, which devotes a blocklength n to creating Y_1, \ldots, Y_n and clock. The size of the identification code obtained is of order $e^{e^{H(Y)n}}$! Making a best choice of X one gets the second order rate $C_F = \max_X H(Y)$, and the identification works if Shannon's transmission capacity $C_{Sh} = \max_X (H(Y) - H(Y|X))$ is positive.

Now the second idea was to wonder whether there is also or can be constructed also a random experiment (or process) in the original case of no feedback in [34], where the second order identification capacity equals C_{Sh} . Well, just choose a transmission λ -code $\{(u_i, D_i): 1 \le i \le exp\{(C_{Sh} - \delta)n\}\}$ and define X^n as the RV taking codewords as values with equal probabilities.

Thus of course the sender knows X^n , but the receiver knows it almost, namely with an error probability not exceeding λ , if he uses the decoding sets D_i . This slight deviation from exact knowledge was not essential, the described experiment in conjunction with the Transformator Lemma below gave a second proof of the direct part of the coding theorem in [34].

This discovery was followed up by [41] and led to solutions of identification problems for multi-way channels with noiseless feedback. The paper contains a novel method to prove weak converses by exploiting Schur concavity of the entropy function. In addition it has two new features, firstly it settles a rather rich class of channel models unheard of in multi-user theory for transmission, where it can be said—"cum grano salis"—that after struggles of more than 30 years the frontiers could not be moved very far beyond [4], secondly the identification schemes are all **constructive** modulo the production of rich random experiments. This richness is measured by what was called **Mystery Numbers** or **Regions of** *k***-tuples of Mystery Numbers** in [41].

The constructions are based on Freivald's Lemma for hashing. As byproduct it gives also a constructive scheme for deterministic channels because they automatically have feedback. Shortly thereafter another construction was given for these special channels in [108].

In dealing with different kinds of feedback strategies it is convenient to have the following concept. Let $\mathcal{F}_n(n=1,2,\dots)$ be a subset of the set of all randomized feedback strategies \mathcal{F}_n^r of a DMC W with blocklength n and let it contain the set \mathcal{F}_n^d of all deterministic strategies.

We call $(\mathcal{F}_n)_{n=1}^{\infty}$ a smooth class of strategies if for all $n_1, n_2 \in \mathbb{N}$ and $n = n_1 + n_2$

$$\mathcal{F}_n \supset \mathcal{F}_{n_1} \times \mathcal{F}_{n_2} \tag{1}$$

where the product means concatenation of strategies.

For $f^n \in \mathcal{F}_n$ the channel induces an output sequence $Y^n(f^n)$. For any smooth class we define numbers

$$\mu(\mathcal{F}_n) = \max_{f^n \in \mathcal{F}_n} H(Y^n(f^n))$$

By (1) and the memoryless character of the channel

$$\mu(\mathcal{F}_n) \geq \mu(\mathcal{F}_{n_1}) + \mu(\mathcal{F}_{n_2}),$$

and therefore

$$\mu = \mu((\mathcal{F}_n)_{n=1}^{\infty}) = \lim_{n \to \infty} \frac{1}{n} \mu(\mathcal{F}_n)$$
 exists.

It was called **mystery number** in [41] and has subsequently been called by us in lectures and papers, in particular also in [13], **common randomness capacity**.

The common randomness capacity C_{CR} is the maximal number ν such, that for a constant c>0 and for all $\epsilon>0$, $\delta>0$ and for all n sufficiently large there exists a permissible pair (K,L) of random variables of length n on a set K with $|K| < e^{cn}$ with

$$Pr\{K \neq L\} < \epsilon \text{ and } \frac{H(K)}{n} > \nu - \delta.$$

From common randomness (also called shared randomness in physics) to identification: The \sqrt{n} -trick

Let $[M] = \{1, 2, ..., M\}$, $[M'] = \{1, 2, ..., M'\}$ and let $\mathcal{T} = \{T_i : i = 1, ..., N\}$ be a family of maps $T_i : [M] \rightarrow [M']$ and consider for i = 1, 2, ..., N the sets

$$K_i = \{(m, T_i(m)) : m \in [M]\}$$

and on $[M] \times [M']$ the PD's

$$Q_i((m,m')) = \frac{1}{M} \text{ for all } (m,m') \in K_i.$$

Transformator Lemma Given $M, M' = \exp\{\sqrt{\log M}\}$ and $\epsilon > 0$ there exists a family $T = T(\epsilon, M)$ such that $|T| = N \ge \exp\{M - c(\epsilon)\sqrt{\log M}\}$, $Q_i(K_i) = 1$ for i = 1, ..., N, and $Q_i(K_j) \le \epsilon \ \forall i \ne j$.

Note In typical applications the common random experiment has range $M = \exp\{C_R n\}$ and uses for its realization the blocklength n, while for the extension to the T_i the blocklength \sqrt{n} suffices.

A further enlightening development concerned what we formulated as a **PRINCIPLE**:

Second order identification capacity equals (first order) common randomness capacity

After [34], [35], and [41] a lot spoke for it and it became a driving dream leading to many results like [47], where the remarkable fact, that a wire-tapper cannot reduce identification capacity, if he cannot prohibit identification for 2 alternatives, and otherwise the identification capacity equals zero, was discovered and proved by arguments, which are by no means simple.

The same paper also started the investigation of identification in the presence of noisy (passive) feedback channels. This is discussed in [13].

Continuing the line of children of the principle there are [30] and striking work on the AVC in [22] and on the arbitrarily varying MAC in [23], [24], and above all for the maximal error concept for the AVC with complete feedback in [25] a determination of the capacity formula, which has a **trichotomy**.

Let's recall that the Ahlswede-dichotomy was for average error and no feedback [6].

What was called "correlation in random codes", originally introduced in the pioneering paper [57], can now be **understood as common randomness**.

Also its elimination in [6] is an early version of what now Computer Scientists call **derandomization**.

Finally, we report on the removal of another heavy stone. Having understood how correlation in random codes, a form of common randomness, helps the communicators for AVC a next question is how a Slepian/Wolf type correlated source (U^n, V^n) [102] helps the identification for a DMC W, when the sender knows U^n and the receiver knows V^n . Well, the principle says that it should be equivalent to asking how much common randomness can the communicators extract from (U^n, V^n) , if they are assisted by the DMC W with capacity $C_{Sh}(W)$.

Now just notice that the case $C_{Sh}(W) = 0$ leads to the problem of finding what I. Csiszar asked for, and according to [115] also D. Slepian, and named **Common Information**. It was determined by P. Gács and J. Körner [73]. As expressed in their title the question was to know how this common information relates to Shannon's

mutual information, in particular whether they are equal.

As we know the quantities are far apart, and under natural conditions, $C_{GK}(U,V)$ equals zero and it only depends on the positions of positivity of the joint distribution P_{UV} .

This got A. Wyner started, who believed that the quantity $C_W(U,V)$ he introduced was the right notion of common information. For one thing it does depend on the actual values of P_{XY} . On the other hand it satisfies $C_W(U,V) \geq I(U \wedge V)$ and is therefore rather big. The authors of [40] gave a critical analysis about the problems at hand.

By the foregoing it is clear that the common randomness capacity of R. Ahlswede and V. Balakirsky, say $C_{AB}^W(U,V)$, equals $C_{GK}(U,V)$, if $C_{Sh}(W)=0$. However, if $C_{Sh}(W)>0$ $C_{AB}^W(U,V)$ nicely depends on the actual value of P_{UV} . Furthermore, $C_{GK}(U,V)$, which was always considered to be somewhat outside Information Theory proper, turns out to be a common randomness capacity. The proof of the characterization of $C_{AB}^W(U,V)$ is a natural extension of the one in case $C_{Sh}(W)=0$ given in [40].

More importantly we feel that the analysis and discussion in [40] are still of interest today.

The first systematic investigation of common randomness started in [31] and was continued after ideas had matured with [32], in particular, with a revival of another old friend: balanced coloring for hypergraphs ([7], [8]).

Very remarkable work has been done since then by Csiszár and Narayan ([64], [65]), and we are particular intrigued by the work of Venkatesan and Anantharam [105], [106].

In conclusion of the subject, we mention that common randomness and entanglement go into the center of Quantum Information Theory. But there according to [111] already for simple channels identification and common randomness can be far apart.

The exploration of new concepts, ideas and models does not end at the discovery of identification. It actually was a starting point for them. We mentioned already that in [13] more general communication systems were introduced and studied.

We have explained the role of common randomness for identification (The Principle!).

In the absence of feedback, one possibility to achieve the maximal possible rate of such a common random experiment is that the sender performs a uniform random experiment and transmits the result to the receiver using an ordinary transmission code. If noiseless feedback is available, the sender sends letters in such a way, that the entropy of the channel output (which he gets to know by the feedback channel) is maximized, where he can either use a deterministic or randomized input strategy, depending on the kind of code he may use. This interpretation proved to be the right one also for other kind of channels like the multiple access channel (see [41]).

State of knowledge about Capacity Regions

For identification the letter D indicates a deterministic encoding and its absence refers to randomized encoding. (For a refined analysis with maximal versus average error probability we refer to [6].)

	Transmission	Identification	
DMC	X	X [34]	
MAC	X	X [13], [103]	
ВС	?	X [13]	
TWC	?	?	
	With Feedback Transmission	Identification	
DMC	X	X [35]	
MAC	?	X D [41]	
MAC	?	?	
ВС	?	? D	
ВС	?	X [41]	
TWC	?	X D [41]	

There are amazing dualities between transmission and identification. For instance concerning feedback there is a rather unified theory of Multi-user identification with feedback—with constructive solutions, whereas for transmission with feedback most capacity regions are unknown. Furthermore using randomness mystery numbers regions are known for the BC, but not for the MAC, whereas, as is well known, for transmission capacity regions the situation is reversed.

Actually common randomness corresponds to the key space in cyptography (see [53]). There are many open entropy characterisation problems: for instance to **calculate** the maximal output entropy $\sup_n \max \frac{1}{n} H(Z^n)$ of a MAC, if $X_{n+1} = f_{n+1}(Z^n)$, $Y_{n+1} = g_{n+1}(Z^n)$ define the encoding processes.

Comparison of identification rate and common randomness capacity: Identification rate can exceed common randomness capacity and vice versa

One of the observations was that random experiments, to whom the communicators have access, essentially influence the value of the identification capacity C_I . Actually, if sender and receiver have a common random capacity C_R then by the Transformator

Lemma always

$$C_I \ge C_R$$
 if $C_I > 0$.

For many channels, in particular for channels with feedback, equality has been proved.

It seemed therefore plausible, that this is always the case, and that the theory of identification is basically understood, when common random capacities are known.

We report here a result, which shows that this expected unification is not valid in general—there remain two theories.

Example 4
$$C_I = 1$$
, $C_R = 0$. (Fundamental)

We suse a Gilbert type construction of error correcting codes with constant weight words. This was done for certain parameters. The same arguments give for parameters needed here the following auxiliary result.

Proposition. Let \mathcal{Z} be a finite set and let $\lambda \in (0, 1/2)$ be given. For $\varepsilon < (2^{2/\lambda} + 1)^{-1}$ a family A_1, \ldots, A_N of subsets of \mathcal{Z} exists with the properties

$$|A_i| = \varepsilon |\mathcal{Z}|, |A_i \cap A_i| < \lambda \varepsilon |\mathcal{Z}| \ (i \neq j)$$

and

$$N \ge |\mathcal{Z}|^{-1} 2^{\lfloor \varepsilon |\mathcal{Z}| \rfloor} - 1.$$

Notice that $\lambda \log(\frac{1}{3} - 1) > 2$ and that for ℓ with $2^{-\ell} = \varepsilon$ necessarily $\ell > \frac{2}{\lambda}$.

Choose now $\mathcal{Z} = \{0,1\}^n$, $\varepsilon = 2^{-\ell}$ and A_i 's as in the Proposition. Thus $|A_i| = 2^{n-\ell}$, $N(n,\lambda) = 2^{-n} 2^{2^{n-\ell}} - 1$ and $|A_i \cap A_j| < \lambda 2^{n-\ell}$.

Consider now a discrete channel $(W^n)^\infty$, where the input alphabets $\mathcal{X}_t = \{1, 2, \dots, N(t, \lambda)\}$ are increasing, $\mathcal{X}^n = \prod_{t=1}^n \mathcal{X}_t$ are the input words of length n, $\mathcal{Y}^n = \{0, 1\}^n$ are the output words and $W^n : \mathcal{X}^n \leadsto \mathcal{Y}^n$ is defined by

$$W^n(\cdot|i_1i_2\ldots i_n)=W^n(\cdot|i_n)$$

and $W^n \cdot (\cdot | i)$ is the uniform distribution on A_i for $1 \le i \le N(n, \lambda)$.

By the Proposition and $3/\lambda > \ell > 2/\lambda$

$$N(n,\lambda) > 2^{-n}2^{2^{n-3/\lambda}}$$

and

$$\underline{\lim}_{n\to\infty}\frac{1}{n}\log\log N(n,\lambda)\geq 1.$$

However, for transmission every decoding set is contained in some A_i and for error probability λ must have cardinality $(1-\lambda)|A_i|=(1-\lambda)2^{n\ell}$.

Therefore $M(n,\lambda) \leq \frac{2^n}{(1-\lambda)2^{n-\ell}} \leq 2^{\ell+1}$, if $\lambda < 1/2$, and $\frac{1}{n} \log M$ $(n,\lambda) \leq \frac{\ell+1}{n} \leq \frac{3/\lambda+1}{n} \to 0 (n \to \infty)$. The transmission capacity is 0. Consequently also $C_R = 0$.

In [86] Kleinewächter presents a counterexample for the other direction. For given real numbers C_{ID} and C_{CR} with $0 < C_{ID} < C_{CR}$, he constructed a discrete channel with memory and noiseless passive feedback with identification capacity C_{ID} and common randomness capacity C_{CR} . This channel is constructed in such a way that it can be used in two ways. In one respect, the channel is good for the generation of common randomness, in the other it is suitable for identification.

IV "Consequences" for Secrecy Systems

Characterisation of the capacity region for the BC for identification

We need the direct part of the ABC Coding Theorem for transmission ([59], [109], [87]).

Here, there are separate messages for decoder $\mathcal Y$ (resp. $\mathcal Z$) and common messages for both decoders.

Achievable are (with maximal errors)

$$\mathcal{T}_{\mathcal{Y}} = \{ (R_{\mathcal{Y}}, R_0) : R_0 \le I(U \land Z), R_0 + R_{\mathcal{Y}}$$

$$\le \min[I(X \land Y), I(X \land Y|U) + I(U \land Z)],$$

$$U \ominus X \ominus YZ, \quad ||U|| \le |\mathcal{X}| + 2 \}$$

resp.

$$\mathcal{T}_{\mathcal{Z}} = \{ (R_0, R_{\mathcal{Z}}) : R_0 \le I(U \land Y), R_0 + R_{\mathcal{Z}}$$

$$\le \min[I(X \land Z), I(X \land Z|U) + I(U \land Y)],$$

$$U \ominus X \ominus YZ, \quad ||U|| \le |\mathcal{X}| + 2 \}.$$

This is our surprising result.

Theorem For the (general) BC the set of achievable pairs of second order rates for identification is given by

$$\begin{split} \mathcal{B} &= \mathcal{T}_{\mathcal{Y}}' \cup \mathcal{T}_{\mathcal{Z}}', \text{ where } \mathcal{T}_{\mathcal{Y}}' = \{(R_{\mathcal{Y}}', R_{\mathcal{Z}}') : \exists (R_{\mathcal{Y}}, R_0) \in \mathcal{T}_{\mathcal{Y}} \\ & \text{with } R_{\mathcal{Y}}' = R_{\mathcal{Y}} + R_0, R_{\mathcal{Z}}' = R_0 \} \text{ and } \\ \mathcal{T}_{\mathcal{Z}}' &= \{(R_{\mathcal{Y}}', R_{\mathcal{Z}}') : \exists (R_0, R_{\mathcal{Z}}) \in \mathcal{T}_{\mathcal{Z}} \\ & \text{with } R_{\mathcal{Y}}' = R_0, R_{\mathcal{Z}}' = R_0 + R_{\mathcal{Z}} \}. \end{split}$$

Remark \mathcal{B} gives also the achievable pairs of first order rates for common randomness. Proof goes via identification!

Remark The theorem has an important consequence. Whereas for one-way channels the common randomness capacity equals the transmission capacity and the transmission capacity region is still unknown for general broadcast channels we know now its common randomness capacity region, where common random experiments for \mathcal{X} -encoder and \mathcal{Y} -decoder and, simultaneously, for \mathcal{X} -encoder and \mathcal{Z} -decoder are generated. Indeed it equals the second order identification capacity region!

That the latter includes the former is clear from our proof of the direct part. The reverse implication follows indirectly by the same argument.

Interesting here is that the outer bound for the common randomness capacity region is proved via identification.

The situation changes, if constraints like independency or security are imposed on the two common random experiments.

A transmission code with rates $(R_{\mathcal{Y}}, R_{\mathcal{Z}})$ can be used for independent common random experiments and thus the transmission capacity region for the general broadcast channel is contained in the identification capacity region.

Furthermore, the identification capacity region $T'_{\mathcal{Y}} \cup T'_{\mathcal{Z}}$ is convex, because it equals the common randomness capacity region for which time sharing applies and thus convexity is given.

Transmission, identification and common randomness capacities for wire-tape channels with secure feedback from the decoder

Recall that wire-tap channels were introduced by A. D. Wyner [114] and were generalized by I. Csiszár and J. Körner [62]. Its identification capacity was determined by R. Ahlswede and Z. Zhang in [47].

Now by secure feedback we mean that the feedback is noiseless and that the wire-tapper has no knowledge about the content of the feedback except via his own output.

Lower and upper bounds to the **transmission capacity** are derived. The two bounds are shown to coincide for two families of degraded wire-tap channels, including Wyner's original version of the wire-tap channel.

The **identification** and **common randomness** capacities for the channels are completely determined.

Also here again identification capacity is much bigger than common randomness capacity, because the common randomness used for the (secured) identification needs not to be secured!

V Analysis of a specific model: K-identification

A relation to standard identification

For reasons, which become apparent soon, we assume *K* to grow

exponentially in the blocklength n, that is,

$$K=2^{\kappa\cdot n}$$
,

where κ is a first order rate.

As for the standard identification problem $(K = 1, \kappa = 0)N$ can grow double exponentially, that is,

$$N = 2^{2^{Rn}}, R > 0$$

where *R* is a second order rate.

The pair (R,κ) is achievable, if for any $\lambda>0, \delta>0$ and all sufficiently large n $(n,2^{2^{(R-\delta)n}},2^{(\kappa-\delta)n},\lambda)$ –codes exist.

Theorem For every DMC the set K of all achievable rate pairs satisfies

(i)
$$\{(R, \kappa): 0 \leq R, \kappa, R + 2\kappa \leq C_{sh}\} \subset \mathcal{K}$$

(ii)
$$\{(R, \kappa) : 0 \le R, \kappa, R + \kappa \le C_{sh}\} \supset \mathcal{K}$$

(iii) For a noiseless DMC there is equality in (i).

In general?

There is a very important connection to r-cover–free families. A family of sets \mathcal{F} is called r-cover-free if $A_0 \not\subset A_1 \cup A_2 \cup \cdots \cup A_r$ holds for all distinct $A_0, A_1, \ldots, A_r \in \mathcal{F}$. Let M(n, r) denote the maximum cardinality of such an \mathcal{F} over an n-element underlying set. This notion was introduced in terms of superimposed codes by Kautz/Singleton.

VI Extensions to Classical/Quantum Channels

There has been great progress in recent years with fruitful exchanges between Information Theory and Physics.

Since most readers are not familiar with this we just **give classical methods which extend or have analoga.**

We prove in [20] that the average error capacity C_q of a quantum arbitrarily varying channel (QAVC) equals 0 or else the random code capacity \bar{C} (Ahlswede's dichotomy). We also establish a necessary and sufficient condition for $C_q > 0$.

It is interesting to note, that in our proof of this we essentially use the **elimination technique** (an early candidate of what is now called derandomization in Computer Sciences) from [18]. There a necessary and sufficient condition for positivity of the capacity was given, if the set of transmission matrices is row-convex closed—that is under a practically satisfactory assumption of robustness. The mathematical problem of characterizing positivity without this assumption in terms of symmetrizability was started in [69] and completely solved in [63] with a non-standard decoding rule and without use of the elimination technique.

On the other hand in the present quantum case we have not

found a suitable decoding rule and follow the elemination technique. Analogously the positivity problem for the QAVC can be settled by reducing it to a **related classical AVC** to which then the result of [63] can be applied.

We emphasize that the very hard maximal error capacity problem for AVC (including Shannon's zero error capacity problem as special case) is based on a more realistic communication model. It was solved for a nice class of channels in [9], where for the first time in the area of AVC a non-standard decoding rule was used. Extension to QAVC constitute a challenging problem!

A hypergraph covering lemma useful for deriving capacity results

- in the theory of identification
- in the theory of common randomness

Lemma Let $\Gamma = (\mathcal{V}, \mathcal{E})$ be a hypergraph, with a measure Q_E on each edge E, such that $Q_E(v) \leq \eta$ for all $E, v \in E$. For a probability distribution P on \mathcal{E} define

$$Q = \sum_{E \in \mathcal{E}} P(E)Q_E,$$

and fix $\epsilon, \tau > 0$. Then there exist vertices $V_0 \subset V$ and edges $E_1, \ldots E_L \in \mathcal{E}$ such that with

$$\bar{Q} = \frac{1}{L} \sum_{i=1}^{L} Q_{E_i}$$

the following holds:

$$Q(\mathcal{V}_0) \leq \tau, \ \forall v \in \mathcal{V} \backslash \mathcal{V}_0 \ (1 - \epsilon) Q(v) \leq \bar{Q}(v) \leq (1 + \epsilon) Q(v),$$

$$L \le 1 + \eta |\mathcal{V}| \frac{2 \ln 2 \log(2|\mathcal{V}|)}{\epsilon^2 \tau}.$$

Remark The lemma applies also to identification for (classical) quantum channels (Ahlswede/Winter [43]).

The blowing up technique

We define the *k*–Hamming–neighbourhood $\Gamma^k B$ of a set $B \subset \mathcal{Y}^n$ as

$$\Gamma^k B \triangleq \{y^n \in \mathcal{Y}^n : d(y^n, y^n) < k \text{ for some } y^n \in B\}$$

where $d(y^n, y'^n) \triangleq (\{t : 1 < t < n, y'_t \neq y_t\}).$

Blowing up Lemma (Ahlswede/Gács/Körner, 1976, [36])

For any DMC W there is a constant c(W): $\forall x^n \in \mathcal{X}^n, B \subset \mathcal{Y}^n$ $W^n(\Gamma^k B | x^n) \ge \Phi(\Phi^{-1}(W^n(B | x^n))) + n^{-1/2}(k-1)c$ if $\Phi(t) = \int_{-\infty}^t (2\pi)^{-1/2} e^{-u^2/2} du$.

Remark We have no quantum version!

A wringing technique

useful for

- strong converse for multi-user channels
- converses for multiple-descriptions in rate-distortion theory

Lemma Let P and Q be probability distributions on \mathcal{X}^n such that for a positive constant c

(1)
$$P(x^n) \le (1+c)Q(x^n)$$
 for all $x^n \in \mathcal{X}^n$,

then for any $0 < \gamma < c$, $0 \le \epsilon < 1$ there exist $t_1, \ldots, t_k \in \{1, \ldots, n\}$, where $0 \le k \le \frac{c}{\gamma}$, such that for some $\bar{x}_{t_1}, \ldots, \bar{x}_{t_k}$

- (2) $P(x_{t_1}|\bar{x}_{t_1},\ldots,\bar{x}_{t_k}) \leq \max((1+\gamma)Q(x_i|\bar{x}_{t_1},\ldots,\bar{x}_{t_k}),\epsilon)$ for all $x_t \in \mathcal{X}$ and all $t = 1, 2, \ldots, n$ and
- (3) $P(\bar{x}_{t_1},\ldots,\bar{x}_{t_k}) \geq \epsilon^k$

Remark Presently only method to prove strong converse for transmission for (classical) **quantum** multiple-access channel (Ahlswede/Cai [28]).

VII Source Coding for Identification: a Discovery of Identification Entropy

Shannon's Channel Coding Theorem for Transmission is paralleled by a Channel Coding Theorem for Identification. We introduced noiseless source coding for identification and suggested the study of several performance measures.

Interesting observations were made already for uniform sources $P_N = (\frac{1}{N}, \dots, \frac{1}{N})$, for which the worst case expected number of checkings $L(P_N)$ (defined in the next column) is approximately 2. Actually it has been shown that

$$\lim_{N\to\infty} L(P_N) = 2.$$

Recall that in channel coding going from transmission to identification leads from an **exponentially** growing number of manageable messages to **double exponentially** many.

Now in source coding roughly speaking the range of average code lengths for data compression is the interval $[0,\infty)$ and it is [0,2) for an average expected length of optimal identification procedures.

Note that no randomization has to be used here.

A discovery is an identification entropy, namely the functional

$$H_I(P) = 2\left(1 - \sum_{u=1}^{N} P_u^2\right)$$

for the source (\mathcal{U}, P) , where $\mathcal{U} = \{1, 2, ..., N\}$ and $P = (P_1, ..., P_N)$ is a probability distribution.

Its operational significance in identification source coding is similar to that of classical entropy H(P) in noiseless coding of data: it serves as a good bound.

Noiseless identification for sources and basic concept of performance

For the source (\mathcal{U}, P) let $C = \{c_1, \dots, c_N\}$ be a binary prefix code (PC) with $||c_u||$ as length of c_u .

Introduce the RV U with $\text{Prob}(U = u) = P_u$ for $u \in \mathcal{U}$ and the RV C with $C = c_u = (c_{u1}, c_{u2}, \dots, c_{u\|u\|})$ if U = u.

We use the PC for noiseless identification, that is user u wants to know whether the source output equals u, that is, whether C equals c_u or not.

He iteratively checks whether $C = (C_1, C_2, ...)$ coincides with c_u in the first, second etc. letter and stops when the first different letters occur or when $C = c_u$. What is the expected number $L_C(P, u)$ of checkings?

Related quantities are

$$L_C = \max_{1 \le u \le N} L_C(P, u),$$

that is, the expected number of ckeckings for a person in the **worst case**, if code *C* is used,

$$L(P) = \min_{C} L_{C}(P),$$

the expected number of checkings in the worst case for the best code, and finally, if **users are chosen by a RV** V independent of U and defined by $\text{Prob}(V = v) = Q_v$ for $v \in V = U$, we consider

$$L_{C}(P,Q) = \sum_{v \in \mathcal{U}} Q_{v} L_{C}(P,v)$$

the average number of expected checkings, if code *C* is used, and also

$$L(P, Q) = \min_{C} L_{C}(P, Q)$$

the average number of expected checkings for a best code.

A natural special case is the mean number of expected checkings

$$\bar{L}_C(P) = \sum_{u=1}^N \frac{1}{N} L_C(P, u),$$

which equals $L_C(P, Q)$ for $Q = (\frac{1}{N}, \dots, \frac{1}{N})$, and

$$\bar{L}(P) = \min_{C} \bar{L}_{C}(P)$$

Another special case of some "intensive appeal" is the case Q=P. Here we write

$$L(P, P) = \min_{C} L_{C}(P, P).$$

It is known that Huffman codes minimize the expected code length for PC.

This is not the case for L(P) and the other quantities in identification. It was noticed already in [13], [17] that a construction of code trees balancing probabilities like in the Shannon–Fano code is often better. In fact the Theorem of [17] establishes that L(P) < 3 for every $P = (P_1, \ldots, P_N)$!

Still it is also interesting to see how well Huffman codes do with respect to identification, because of their classical optimality property.

Examples for Huffman codes

We start with the uniform distribution

$$P^{N} = (P_{1}, \dots, P_{N}) = \left(\frac{1}{N}, \dots, \frac{1}{N}\right),$$

$$2^n \le N < 2^{n+1}.$$

Then $2^{n+1} - N$ codewords have the length n and the other $2N - 2^{n+1}$ other codewords have the length n+1 in any Huffman code. We call the $N-2^n$ nodes of length n of the code tree, which are extended up to the length n+1 **extended nodes**.

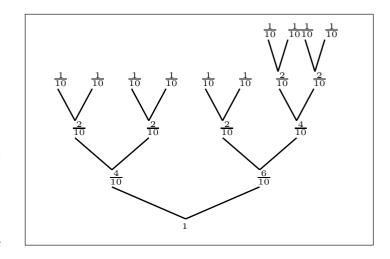
All Huffman codes for this uniform distribution differ only by the positions of the $N-2^n$ extended nodes in the set of 2^n nodes of length n.

The average codeword length (for transmission) does not depend on the choice of the extended nodes.

However, the choice influences the performance criteria for identification!

Example 5 N = 10. There are $\binom{2^3}{10-2^3} = 28$ Huffman codes.

The 4 worst Huffman codes are maximally unbalanced.

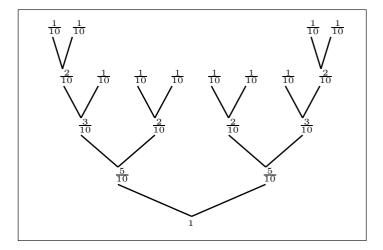


Here

$$L_{\mathcal{C}}(P) = 1 + 0.6 + 0.4 + 0.2 = 2.2$$

 $L_{\mathcal{C}}(P, P) = \frac{1}{10}[1.6 \cdot 4 + 1.8 \cdot 2 + 2.2 \cdot 4] = 1.880.$

One of the 16 best Huffman codes



Here

$$L_{\mathcal{C}}(P) = L_{\mathcal{C}}(\tilde{c}) = 1 + 0.5 + 0.3 + 0.2 = 2.000$$

 $L_{\mathcal{C}}(P, P) = \frac{1}{5}(1.7 \cdot 2 + 1.8 \cdot 1 + 2.0 \cdot 2) = 1.840$

Remark Notice that Shannon's data compression gives $H(P) + 1 = \log 10 + 1 > \sum_{n=1}^{10} P_n \|C_n\| = \frac{1}{10} \cdot 3 \cdot 6 + \frac{1}{10} \cdot 4 \cdot 4 = 3$ $\frac{2}{5} \ge \log 10$

Theorem For every source (\mathcal{U}, P^N)

$$L(P^N) \ge L(P^N, P^N) \ge H_I(P^N).$$

Theorem For $P^N = (P_1, \dots, P_N)$

$$\bar{L}(P^N) \le 2\left(1 - \frac{1}{N^2}\right).$$

Theorem For $P^N = (2^{-\ell_1}, \dots, 2^{-\ell_N})$ with 2-powers as probabilities

$$L(P^N, P^N) = H_I(P^N).$$

Theorem

$$L(P^N, P^N) \le 2\left(1 - \sum_{u} \left(\sum_{s=1}^{\alpha(u)} P_{us}^2\right)\right) \le 2\left(1 - \frac{1}{2}\sum_{u} P_u^2\right).$$

For $P_u = \frac{1}{N}(u \in \mathcal{U})$ this gives the upper bound $2(1 - \frac{1}{2}N)$, which is better than the bound $2(1 - \frac{1}{N^2})$ for uniform distributions.

Finally we derive

Corollary

$$L(P^N, P^N) \le H_I(P^N) + \max_{1 \le u \le N} P_u.$$

It shows the lower bound of $L(P^n, P^N)$ by $H_I(P^N)$ and this upper bound are close.

Further Remarks

1. Our results can be extended to *q*-ary alphabets, for which then identification entropy has the form

$$H_{I,q}(P) = \frac{q}{q-1} \left(1 - \sum_{u=1}^{N} P_u^2 \right).$$

2. Tsallis generalized Boltzmann's entropy

$$H(P) = -k \sum P_u ln P_u$$

to

$$S_{\alpha}(P) = k \frac{1}{\alpha - 1} \left(1 - \sum_{u=1}^{N} P_{u}^{\alpha} \right)$$

for any real $\alpha \neq 1$.

Clearly $\lim_{\alpha \to 1} S_{\alpha}(P) = H(P) = S_1(P)$, say.

One readily verifies that for product-distributions $P \times Q$ for independent random variables

$$S_{\alpha}(P \times Q) = S_{\alpha}(P) + S_{\alpha}(Q) - \frac{(\alpha - 1)}{k} S_{\alpha}(P) S_{\alpha}(Q).$$

Since in all cases $S_{\alpha} \ge 0$, $\alpha < 1$, $\alpha = 1$ and $\alpha > 1$ respectively correspond to **superadditivity**, **additivity and subadditivity** (also called for the purposes in statistical physics **superextensitivity**, **extensitivity**, and **subextensitivity**).

We have been told by several experts in physics that the operational significance of the quantities S_{α} (for $\alpha \neq 1$) in statistical physics seems not to be undisputed.

In contrast we have demonstrated the significance of identification entropy, which is formally close, but essentially different for two reasons: always $\alpha=2$ and $k=\frac{q}{q-1}$ is uniquely determined and depends on the alphabet size q!

3. In [26] we have discussed the coding theoretical meanings of the factors $\frac{q}{q-1}$ and $(1-\sum_{u=1}^N P_u^2)$.

In particular we have the

Theorem For a DMS $(U^n,V^n)_{n=1}^{\infty}$ with generic distribution $P_{UV}=PQ$, i.e. the generic random variables U and V are independent and $P_U=P$, $P_V=Q$

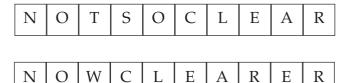
$$\lim_{n\to\infty} L(P^n, Q^n) = \begin{cases} 1 & \text{if } P \neq Q \\ \frac{q}{q-1} & \text{if } P = Q. \end{cases}$$

B. Combinatorial Models

That Combinatorics and Information Sciences often come together is no surprise, because they were born as twins (Leibniz in Ars Combinatoria gives credit to Raimundus Lullus from Catalania, who wanted to create a formal language).

VIII Updating Memories with Cost Constraints: Optimal Anticodes

In the example



d = 7 letters have to be changed for an updating, where d is the Hamming distance, measuring the cost.

How many messages can be updated into each other, if $\cos t \le c$? This is equivalent to the diametric problem in Hamming spaces. It was solved in [39].

For a Hamming space (\mathcal{X}_q^n, d_H) , the set of n-length words over the alphabet $\mathcal{X}_q = \{0, 1, \dots, q-1\}$ endowed with the distance d_H , we determine the maximal cardinality of subsets with a prescribed diameter d or, in another language, anticodes with distance d. We refer to the result as Diametric Theorem.

In a sense anticodes are dual to codes, which have a prescribed

lower bound on the pairwise distance. It is a hopeless task to determine their maximal sizes exactly.

We find it remarkable that the Diametric Theorem (for arbitrary q) can be derived from the Complete Intersection Theorem, which can be viewed as a Diametric Theorem (for q=2) in the constant weight case, where all n-length words considered have exactly k ones.

 \mathbb{N} denotes the set of positive integers and for $i, j \in \mathbb{N}$, i < j, the set $\{i, i+1, \ldots, j\}$ is abbreviated as [i, j]. Moreover, for [1, j] we also write [j]. For $k, n \in \mathbb{N}$, $k \le n$, we set

$$2^{[n]} = \{F : F \subset [1, n]\} \text{ and } \binom{[n]}{k} = \{F \in 2^{[n]} : |F| = k\}.$$

A system of sets $A \subset 2^{[n]}$ is called *t*–intersecting, if

$$|A_1 \cap A_2| \ge t$$
 for all $A_1, A_2 \in \mathcal{A}$,

and I(n, t) denotes the set of all such systems.

Moreover, we define $I(n, k, t) = \{A \in I(n, t) : A \subset {[n] \choose k}\}.$

The investigation of the function $M(n, k, t) = \max_{A \in I(n, k, t)} |A|$, $1 \le t \le k \le n$, and the structure of maximal systems was one of the oldest problems in combinatorial extremal theory and was initiated by Erdös, Ko, and Rado.

They proved already in the year 1938 the following theorem, which was published only in 1961 [68].

Theorem For $1 \le t \le k$ and $n \ge n_0(k, t)$ (suitable)

$$M(n, k, t) = \binom{n-t}{k-t}.$$

Clearly, the system

$$A(n, k, t) = \left\{ A \in \binom{[n]}{k} : [1, t] \subset A \right\}$$

is t-intersecting, has cardinality $\binom{n-t}{k-t}$, and is therefore optimal for $n \ge n_0(k, t)$.

The smallest $n_0(k, t)$, for which this is the case, has been determined by Frankl 1978 in [72] for $t \ge 15$ and subsequently 1984 in [110] for all t:

$$n_0(k, t) = (k - t + 1)(t + 1).$$

We have settled all the remaining cases: n < (k - t + 1)(t + 1).

Complete Intersection Theorem [38] Define $\mathcal{F}_i =$

 $\{F \in {[n] \choose k}: |F \cap [1, t+2i]| \ge t+i\}$ for $0 \le i \le \frac{n-t}{2}$. For $1 \le t \le k \le n$ with

(i)
$$(k-t+1)(2+\frac{t-1}{r+1}) < n < (k-t+1)(2+\frac{t-1}{r})$$
 for some $r \in \mathbb{N} \cup \{0\}$

we have

$$M(n, k, t) = |\mathcal{F}_r|$$

and \mathcal{F}_r is—up to permutations—the unique optimum. By convention $\frac{t-1}{r}=\infty$ for r=0.

(ii)
$$(k-t+1)(2+\frac{t-1}{r+1}) = n \text{ for } r \in \mathbb{N} \cup \{0\}$$

we have

$$M(n, k, t) = |\mathcal{F}_r| = |\mathcal{F}_{r+1}|$$

and an optimal system equals—up to permutations—either \mathcal{F}_r or \mathcal{F}_{r+1} .

Remark In particular this proves the so called 4m – *Conjecture* (Erdös, Ko, Rado 1938, [68])

$$M(4m,2m,2) = \left| \left\{ F \in \binom{[4m]}{2m} : F \cap [1,2m] \ge m+1 \right\} \right|.$$

Remarks Our most recent results on intersecting families can be found in [15], which contains many further references, and our most advanced method is the shifting technique of [14]. We also draw attention to the local-global principle [21] which plays a key role in the recent book [79].

For non-constant weight anticodes the complete solution is this.

Diametric Theorem [39] *For* $q \ge 2$ *let* $r \in \{0\} \cup \mathbb{N}$ *be the largest integer such that*

$$n-d+2r < \min\left\{n+1, n-d+2\frac{n-d-1}{q-2}\right\},$$

then

 $\max\{|\mathcal{A}|: \mathcal{A} \subset \mathcal{X}_q^n, diam(\mathcal{A}) \leq d\} = |\{a^n \in \mathcal{X}_\alpha^n: \sum_{s=1}^{n-d+2r} w_H(a_s) \leq r\}|.$

(By convention
$$\frac{n-d-1}{q-2} = \infty$$
 for $q = 2$.)

Another diametric theorem in Hamming spaces concerns optimal group anticodes [12].

A report on Extremal Problems in Number Theory and especially also in Combinatorics, which arose in Information Theory, can be found in [10], [19] and [67].

IX Information Flows in Networks

We continue now with the subject whose origin is generally attributed to [29]. The founder of Information Theory Claude E. Shannon, who set the standards for efficient transmission of channels with noise by introducing the idea of coding also wrote together with Peter Elias and Amiel Feinstein a basic paper on networks [99] discussing algorithmic aspects of the Min Cut—Max Flow Theorem [70], saying that for flows of physical commodities like electric currents or water, satisfying Kirchhoff's laws, the maximal flow equals the minimal cut.

With the stormy development of Computer Science there is an ever increasing demand for designing and optimizing information flows over networks—for instance in the internet.

Data, that is strings of symbols, are to be send from sources s_1, \ldots, s_n to their destinations, sets of node sinks D_1, \ldots, D_n .

Computer scientist quickly realized that it is beneficial to copy incoming strings at processors sitting at nodes of the network and to forward copies to adjacent nodes. This task is called multicasting.

However, quite surprisingly **they did not consider coding**, which means here to produce not only copies, but, more generally, new output strings as deterministic functions of incoming strings.

A Min-Max-Theorem was discovered and proved for information flows by Ahlswede, Cai, Li, and Yeung in [29].

Its statement can be simply explained. For one source only, that is n=1, in the notation above, and $D_1=\{d_{11},d_{12},\ldots,d_{1t}\}$ let F_{1j} denote the max-flow value, which can go for any commodity like water in case of Ford/Fulkerson from s_i to d_{1i} . The same water cannot go to several sinks. However, the amount of $\min_{1\leq j\leq t}F_{1j}$ bits can go **simultaneously** to d_{11},d_{12},\ldots and d_{1t} . Obviously, this is best possible. It has been referred to as ACLY-Min-Max-Theorem. To the individual F_{1j} Ford/Fulkerson's Min-Cut-Max-Flow Theorem applies.

It is very important that in the starting model there is no noise and it is amazing for how long Computer Scientists did the inferior multi-casting allowing only copies. It is perhaps surprising that Shannon seems not to have realized the consequences of the basic difference between classical and information flows. We substantiate this by citing from his Kyoto lecture [98].

"A basic idea in information theory is that information can be treated very much like a physical quantity, such as mass or energy. For example, an information source is like a lumber mill producing lumber at a certain point. The channel might correspond to a conveyor system for transporting the lumber to a second point. In such a situation there are two important quantities: the rate R (in cubic feet per second) at which lumber is produced at the mill and the capacity C (in cubic feet per second) of the conveyor. These two quantities determine whether or not the conveyor system will be adequate for the lumber mill. If the rate of production R is greater than the conveyor capacity C, it will certainly be impossible to transport the full output of the mill; there will

not be sufficient space available. If R is less than or equal to C, it may or may not be possible, depending on whether the lumber can be packed efficiently in the conveyor. Suppose, however, that there is a sawmill at the source. This correspond in the analogy to the encoder or transmitter. Then the lumber can be cut into small pieces in such a way as to fill out the available capacity of the conveyor with 100 percent efficiency. Naturally, in this case a carpenter would be provided at the receiving point to fasten the pieces back together in their original form before passing them on to the consumer.

If this analogy is sound, it should be possible to set up a measure R, in suitable units, giving the rate at which information is produced by a given information source, and a second measure C that determines the capacity of a channel for transmitting information. Furthermore, the analogy would suggest that by a suitable coding or modulation system, the information can be transmitted over the channel if and only if the rate of production R is not greater than the capacity C. A key result of information theory is that it is indeed possible to set up measures R and C having this property."

Network flows with **more than one source** are much harder to analyze and lead to a wealth of old and new combinatorial extremal problems.

Even nicely characterized classes of **error correcting codes** come up as being isomorphic to a complete set of solutions of flow problems **without errors**!

Also optimal anticodes (see theorem above) arise in such a role!

On the classical side for instance orthogonal Latin Squares arise.

It is known that classical network flows have many connections to combinatorial extremal problems like Baranyai's factorization theorem [52] or especially for matching problems. Information flows promise more such connections as for example in [113]. There may be a great challenge not only coming to **Combinatorics** but also to **Algebraic Geometry** and its present foundations.

We draw attention to the chapter on Network Coding in [19], pages 858–897.

X Localized Errors

A famous problem in coding theory consists in finding good bounds for the maximal size, say N(n, t, q), of a t-error correcting code over a q-ary alphabet $Q = \{0, 1, \dots, q-1\}$ with blocklength n.

This code concept is suited for communication over a q-ary channel with input and output alphabets Q, where a word of length n sent by the encoder is changed by the channel in atmost t letters. Here neither the encoder nor the decoder knows in advance where the errors, that is changes of letters, occur.

It is convenient to use the notation relative error $\tau = t/n$ and rate $R = n^{-1} \log M$.

The Hamming bound is an upper bound on it.

$$H_q(\tau) = \begin{cases} 1 - h_q(\tau) - \tau \log_q(q - 1) & \text{if } 0 \le \tau \le \frac{q - 1}{q} \\ 0 & \text{if } \frac{q - 1}{q} < \tau \le 1. \end{cases}$$

We turn now to another model. Suppose that the **encoder**, who wants to encode message $i \in \mathcal{M} = \{1, 2, \dots, M\}$, knows the t-element set $E \subset [n] = \{1, \dots, n\}$ of positions, in which only errors may occur. He then can make the codeword presenting i dependent on $E \in \mathcal{E}_t = {[n] \choose t}$, the family of t-element subsets of [n]. We call them "a priori error pattern". A family $\{u_i(E) : 1 \le i \le M, \ E \in \mathcal{E}_t\}$ of q-ary vectors with n components is an $(M, n, t, q)_l$ code (for localized errors), if for all $E, E' \in \mathcal{E}_t$ and all q-ary vectors $e \in V(E) = \{e = (e_1, \dots, e_n) : e_i = 0 \text{ for } j \notin E\}$ and $e' \in V(E')$

$$u_i(E) \oplus e \neq u_{i'}(E') \oplus e'$$
 for $i \neq i'$,

where \oplus is the addition modulo q.

We denote the capacity error function, that is the supremum of the rates achievable for τ and all large n, by C_q^l . It was determined by Bassalygo/Gelfand/Pinsker [54] for the binary case to equal $H_2(\tau)$. For general q the best known result is

Theorem

(i)
$$C_q^l(\tau) \le H_q(\tau)$$
, for $0 \le \tau \le \frac{1}{2}$.

(ii)
$$C_q^l(\tau) = H_q(\tau)$$
, for $0 \le \tau < \frac{1}{2} - \frac{q-2}{2q(2q-3)}$.

Competing Ideas:

Ahlswede: With increase of q the Hamming space should become more flexible for packing and the Hamming bound should be tight for $0 \le \tau \le \frac{1}{2}$.

Pinsker: Knowing the a-priori error pattern E gives less **protocol** information if q increases.

Who wins?

XI Search

After we wrote with I. Wegener one of the first books on search in 1978, the subject has grown terrifically. **Still progress is possible on basic questions**.

For input alphabet $\mathcal{X}=Q$ and output alphabet $\mathcal{Y}=Q$ let $M_f(n,t,q)$ be the maximal size of a t-error correcting code over a q-ary alphabet with block length n in the presence of noiseless feedback, that means having sent letters $x_1,\ldots,x_{j-1}\in\mathcal{X}$ the encoder knows the letters $y_1,\ldots,y_{j-1}\in\mathcal{Y}$ received before he sends the next letter $x_j(j=1,2,\ldots,n)$. Define the relative error $\tau=t/n$, the rate $R=n^{-1}\log M$, and the capacity error function $C_q^f(\tau)$ as the supremum of the rates achievable for τ and all large

Theorem ([55], [116])

$$C_2^f(\tau) = \begin{cases} h_2(\tau) & \text{if } 0 \le \tau \le \tau_t \\ (-3R_0\tau) + R_0 & \text{if } \tau_t \le \tau \le \frac{1}{3}, \end{cases}$$

where $R_0 = \log_2(\frac{1+\sqrt{5}}{2})$ and $\tau_t = (3+\sqrt{5})^{-1}$.

Theorem ([33]) *Let* $q \ge 3$

(i)

$$C_q^f(\tau) \begin{cases} \leq H_q(\tau) & \text{if } 0 \leq \tau \leq \frac{1}{q} \\ = (1 - 2\tau) \log_q(q - 1) & \text{if } \frac{1}{q} \leq \tau \leq \frac{1}{2} \\ = 0 & \text{if } \frac{1}{2} \leq \tau \leq 1 \end{cases}.$$

(ii) The rate function obtained by the r-rubber method is a tangent to $H_q(\tau)$ going through $(\frac{1}{r+1}, 0)$.

The rubber method

Let $b: \mathcal{M} \to \{1, 2, \dots, q-1\}^{n-2t}$ be a bijection between the messages and the used sequences.

The "0" is used for error correction only.

Given $i \in \mathcal{M}$ the sender chooses $b(i) = (x_1, x_2, ..., x_{n-2t}) \in \{1, 2, ..., q-1\}^{n-2t}$ as a **skeleton for encoding**, which finally will be known to the receiver.

For all positions $i \le n$ not needed dummies $x_i = 1$ are defined to fill the block length n.

Transmission algorithm: The sender sends x_1 , x_2 until the first error occurs, say in position p with x_p sent.

If a **standard error** occurs $(x_p \to y_p \in \{1, 2, ..., q-1\})\}$, the sender transmits, with smallest l possible, 2l+1 times 0 until the decoder received l+1 zeros. Then he transmits at the next step x_p , again, and continues the algorithm.

If a **towards zero error** occurs ($x_p \rightarrow y_p = 0$), the sender decreases p by one (if it is bigger than 1) and continues (transmits at the next step x_p).

Decoding algorithm: The receiver just regards the "0" as a protocol symbol—he erases it by a rubber, **who in addition erases the previous symbol**.

r-rubber method: Let the skeleton defined by $\{x^{n-(r+1)t} \in \{0, 1, \dots, q-1\}^{n-(r+1)t}$: the sequence contains $\leq r-1$ consecutive zeros $\}$ and the protocol string defined as r consecutive zeros.

Relation between Berlekamp's strategies and *r*-rubber method

— For q = 2 and r > 1 the r-rubber strategies have the same rate as Berlekamp's strategies (tangents to the Hamming bound

going through $(\frac{1}{r+1}, 0)$).

- Especially for q = 2 and r = 2 we get Berlekamp's tangent bound.
- More general we get for q > 2 and $r \ge 1$ tangents to the Hamming bound going through $(\frac{1}{r+1}, 0)$.

XII Combi-probabilistic Models: Coloring Hypergraphs did a Problem by Gallager

Slepian/Wolf Model 1973 ([102])

For a DMCS $((X^n, Y^n))_{n=1}^{\infty}$ with alphabets \mathcal{X} and \mathcal{Y} for encoding $f: \mathcal{Y}^n \to \mathbb{N}$ and decoding $g: \mathcal{X}^n \times \mathbb{N} \to \mathcal{X}^n \times \mathcal{Y}^n$ with $Prob(g(X^n, f(Y^n)) = (X^n, Y^n)) \sim 1$ it is true that the optimal rate (f) equals H(Y|X).

Gallager Model 1976 ([75])

For a discrete, memoryless conditional distribution $(\{Y^n(x^n): x^n \in \mathcal{X}^n\})_{n=1}^{\infty}$ (Generic $P_{Y|X}$) with alphabets \mathcal{X} and \mathcal{Y} for encoding $f: \mathcal{Y}^n \to \mathbb{N}$ and decoding $g: \mathcal{X}^n \times \mathbb{N} \to \mathcal{X}^n \times \mathcal{Y}^n$ with $Prob(g(x^n, f(Y^n)) = (x^n, Y^n)) \sim 1 \quad \forall x^n \in \mathcal{X}^n$, we proved that the optimal rate (f) equals $\max_x H(Y|X=x)$.

Here RANDOM SELECTION fails.

Our solution is given already in [1] by a counting argument and in [7] it proceeds by a **combined greedy/random selection**.

C. Further Perspectives

Protocol Information

"Protocol" information we encountered in the Theory of Localized Errors and in the Rubber Method. The subject was started by R.G. Gallager [74] and deserves further investigations.

Beyond Information Theory: Identification as a New Concept of Solution for Probabilistic Algorithms

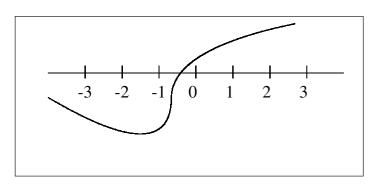
We mention as perhaps one of the most promising directions the study of probabilistic algorithms with identification as *concept of solution and underline its importance by repeating*:

The algorithm should be fast and have small error probabilities. Every algorithmic problem can be thus considered. This goes far beyond Information Theory. Of course, like in general information transfer also here a more general set of questions can be considered. As usual in Complexity Theory one may try to classify problems.

What rich treasures do we have in the much wider areas of information transfer?!

Example 6

Develop probabilistic algorithms which answer very quickly with high probability correctly whether a polynomial $P : \mathbb{R} \to \mathbb{R}$ has a root in the interval [i, i+1] or not, for any $i \in \mathbb{N}$.



A new connection between information inequalities and Combinatorial Number Theory: The final form of Tao's inequality relating conditional expectation and conditional mutual information

Recently Terence Tao approached Szemerédi's Regularity Lemma from the perspectives of Probability Theory and of **Information Theory** instead of Graph Theory and found a stronger variant of this lemma, which involves a new parameter.

To pass from an entropy formulation to an expectation formulation he found the following

Lemma. Let Y, X, and X' be random variables taking values in \mathcal{Y} and \mathcal{X} , respectively, where $\mathcal{Y} \subset [-1,1]$, and with X' = f(X) for a (deterministic) function f. Then we have

$$\mathbb{E}(|\mathbb{E}(Y|X') - \mathbb{E}(Y|X)|) \le 2I(X \wedge Y|X')^{\frac{1}{2}}.$$

We show that the constant 2 can be improved to $(2\ln 2)^{\frac{1}{2}}$ and that this is the best possible constant.

Could we ask Shannon's advice !!!

The following last paragraph on page 350 is taken from "Coding theorems for a discrete source with a fidelity criterion", C. Shannon Collected Papers, 325–350.

"In a somewhat dual way, evaluating the rate-distortion function R(D) for a source amounts, mathematically, to minimizing a mutual Information under variant of the $q_i(j)$, again with a linear inequality constraint. The solution leads to a function R(d) which is convex downward. Solving this problem corresponds to finding a channel that is just right for the source and allowed distortion level. This duality can be pursued further and is related to the duality between past and future and the notions of control and knowledge. Thus we may have knowledge of the past

but cannot control it; we may control the future but have no knowledge of it."

The often cited last sentence, which we put here in boldface, has made several thinkers curious.

We sketch below our ideas about creating order involving knowledge of past and future and wonder what Shannon, whom we never met, would think about them. They are motivated by Clausius' second law of thermodynamics

"Heat cannot by itself pass from a colder to a hotter body."

He also introduced entropy, for which Boltzmann gave a famous formula.

We quote A. Rényi, Probability Theory, North Holland, Amsterdam, p. 554, 1970, for his opinion about this.

"The quantity $\sum_{k=1}^{n} p_k \log_2 \frac{1}{p_k}$ is frequently called the entropy of the distribution $\mathcal{P} = (p_1, \dots, p_k)$. Indeed, there is a strong connection between the notion of entropy in thermodynamics and the notion of information (or uncertainly). L. Boltzmann was the first to emphasize the probabilistic meaning of the thermodynamical entropy and thus he may be considered as a pioneer of information theory. It would even be proper to call the formula the Boltzmann-Shannon formula. Boltzmann proved that the entropy of a physical system can be considered as a measure of the disorder in the system. In case of a physical system having many degrees of freedom (e.g. perfect gas) the number measuring the disorder of the system measures also the uncertainty concerning the states of the individual particles."

Creating order with simple machines

In [45] and [46] a new field of research, creating order in sequence spaces with simple machines, was introduced. People spend a large amount of time creating order in various circumstances. We contribute to a theory of ordering. In particular we try to understand how much "order" can be created in a "system" under constraints on our "knowledge about the system" and on the "actions we can perform in the system".

We have a box that contains β objects at time t labeled with numbers from $\mathcal{X} = \{0, \dots, \alpha - 1\}$. The state of the box is $s_t = (s_t(1), \dots, s_t(\alpha))$, where $s_t(i)$ denotes the number of balls at time t labeled by i.

Assume now that an arbitrary sequence $x^n = (x_1, \dots, x_n) \in \mathcal{X}^n$ enters the box iteratively. At time t an organizer \mathcal{O} outputs an object y_t and then x_t enters the box. $x^n = (x_1, \dots, x_n)$ is called an input and $y^n = (y_1, \dots, y_n)$ an output sequence. The organizer's behavior must obey the following rules.

Constraints on matter. The organizer can output only objects from the box. At each time *t* he must output exactly one object.

Constraints on mind. The organizer's strategy depends on

- (a) his knowledge about the time t. The cases where \mathcal{O} has a timer and has no timer are denoted by T^+ and T^- , respectively.
- (b) his knowledge about the content of the box. O^- indicates that the organizer knows at time t only the state s_t of the box. If he also knows the order of entrance times of the objects, we write O^+ .
- (c) the passive memory (π, β, φ) . At time t the organizer remembers the output letters $y_{t-\pi}, \ldots, y_{t-1}$ and can see the incoming letters $x_{t+1}, \ldots, x_{t+\varphi}$.

Let $\mathcal{F}_n(\pi, \beta, \varphi, T^-, O^-)$ be the set of all strategies for (T^-, O^-) , length n and a given memory (π, β, φ) and \mathcal{S} be the set of all states. A strategy $f_n : \mathcal{X}^n \times \mathcal{S} \to \mathcal{X}^n$ assigns to each pair (x^n, s_1) an output y^n . Denote $\mathcal{Y}(f_n)$ the image of $\mathcal{X}^n \times \mathcal{S}$ under f_n . Also denote $||\mathcal{Y}(f_n)||$ the cardinality of $\mathcal{Y}(f_n)$.

Now we define the size

$$N_{\alpha}^{n}(\pi, \beta, \varphi) = \min\{||\mathcal{Y}(f_n)|| : f_n \in \mathcal{F}_n(\pi, \beta, \varphi, T^-, O^-)\}$$

and the rate

$$\nu_{\alpha}(\pi, \beta, \varphi) = \lim_{n \to \infty} \frac{1}{n} \log N_{\alpha}^{n}(\pi, \beta, \varphi).$$

Analogously, we define in the case (T^-, O^+) the quantities $O^n_{\alpha}(\pi, \beta, \varphi)$, $\omega_{\alpha}(\pi, \beta, \varphi)$, in the case (T^+, O^-) the quantities $T^n_{\alpha}(\pi, \beta, \varphi)$, $\tau_{\alpha}(\pi, \beta, \varphi)$ and in the case (T^+, O^+) the quantities $G^n_{\alpha}(\pi, \beta, \varphi)$, $\gamma_{\alpha}(\pi, \beta, \varphi)$.

(d) the active memory. Now the organizer has additional memory of size m, where he is free to delete or store any relevant information at any time. Here we are led to study the quantities $N_{\alpha}^{n}(\pi, \beta, \varphi, m)$, $\nu_{\alpha}(\pi, \beta, \varphi, m)$, etc.

Survey of the results

π	φ	$v_2(\pi, \beta, \varphi)$
0	0	1
0	1	1
1	0	$\sup_{\delta} (1 - (\beta - 1)\delta) h\left(\frac{\delta}{1 - (\beta - 1)\delta}\right)$
π	∞	$1/\beta$
∞	$\leq \beta - 1$	$\log \lambda^*$, where λ^* is the largest root of $\lambda^{\beta+1+\varphi} = \lambda^{\lceil (\beta+1+\varphi)/2 \rceil} + \lambda^{\lfloor (\beta+1+\varphi)/2 \rfloor}$
∞	$\geq \beta - 1$	$1/\beta$

Furthermore the following relations hold. $\omega_2(\infty, \beta, \varphi) = \nu_2(\infty, \beta, \varphi)$, $\omega_2(\pi, \beta, \infty) = \nu_2(\pi, \beta, \infty)$, $\lim_{\beta \to \infty} \nu_3(0, \beta, 0) = 1$, $\tau_2(\pi, \beta, \varphi) = \nu_2(\infty, \beta, \varphi)$ for $\pi \ge 1$,

$$\tau_2(0, 2, 0) = \log((\sqrt{5} + 1)/2).$$

In the model of active memory we have for the memory size m=2 that $\nu_2(0,\,\beta,\,0,2)=\nu_2(1,\,\beta,\,0)=\log\lambda_\beta$, where λ_β is the positive root of $\lambda^\beta-\lambda^{\beta-1}-1=0$.

The general case, where the size α of the set \mathcal{X} , the size β of the box, and the memory parameters π , φ and m are arbitrary, has not been solved yet. This is the cardinal goal for our research to aim at within this field. We have the following **conjectures**.

- 1. $\lim_{\varphi \to \infty} \nu_2(\pi, \beta, \varphi) \neq \nu_2(\pi, \beta, \infty)$ (in the analogous case for $\pi \to \infty$ equality holds)
- 2. $\lim_{\beta\to\infty} \nu_\alpha(0,\beta,0) = \log_2\lceil(\alpha+1)/2\rceil$ (for $\alpha=2$ and $\alpha=3$ this is true)

3.
$$\omega_2(0, \beta, 0) = \nu_2(1, \beta - 1, 0)$$

In a probabilistic model the objects or letters are produced by a stochastic process, which in the simplest case is a sequence $(X_t)_{t=1}^\infty$ of i.i.d. RV's with values in $\mathcal{X}=\{0,1,\ldots,\alpha-1\}$ and generic distribution P_X . In Information Theory this is also called a discrete, memoryless source. For a strategy f_n , which depends on the triple (π,β,φ) , let $Y^n=Y_1\ldots Y_n$ be the output sequence corresponding to $X^n=X_1\ldots X_n$. Let $F_\alpha^n(\pi,\beta,\varphi,P_X)$ be the set of strategies restricted to block length n.

We use the "per letter" entropy $\frac{1}{n}H(Y^n)$ as performance criterion and define

$$\eta_{\alpha}(\pi, \beta, \varphi, P_X) = \lim_{n \to \infty} \min_{f_n \in F_{\alpha}^n(\pi, \beta, \varphi, P_X)} \frac{1}{n} H(Y^n).$$

This is the smallest mean entropy of the output process, which can be achieved by \mathcal{O} with strategies based on his knowledge. It corresponds to the optimal rate $\nu_{\alpha}(\pi, \beta, \varphi)$ in the non-probabilistic model. Our new quantity is much harder to analyze.

In the first non-trivial case $\beta = 2$ and $\pi = \infty$, $\varphi = 0$ only the simplest non-trivial source, namely the binary symmetric source defined by $P_X(0) = P_X(1) = 1/2$, could be analyzed.

Theorem The strategy which is locally optimal for every $t=1,2,\ldots$ is optimal. Moreover for the disjoint events $D_k=E_k\setminus E_{k+1}$, where $E_k=\{Y^k=01010\ldots\}$, $q(k)=Prob(D_k)$ satisfies $\sum_{n=1}^{\infty}q(k)=1$ and

$$\eta_2(\infty, 2, 0, P_X) = \frac{H(q)}{\sum\limits_{k=1}^{\infty} kq(k)} = 0,5989\dots$$
(2)

Conjecture The formula (2) has a nice structure. It suggests a general principle for arbitrary sources. However, already the binary non-symmetric source is difficult to solve.

Finally we mention the survey of Vanroose, pages 603–613 in [48].

Directions of developments of our basic model for sequences

Multiple in- and outputs: *s* inputs and *s* outputs, varying number of outputs, merging, splitting, correlation

Objects with special features: Varying-length objects, death-birth, idle objects, box with exclusion rule

Compound objects: Box with reaction rules, representatives, objects with many properties, exchanging parts of objects

Errors: Probabilistic, confusion rule, frequency rule, receiver can distinguish only certain objects

Applications

Production of goods, arrival of goods and documents, garbage collection

Extensions of the basic model

A combined theory of ordering and source coding

Ordering, sorting and Maxwell's demon

A calculus of machines: comparisons of machines, commutativity

Other topics

When after an interruption of a decade we attended the ISIT again, namely in Seattle 2006, we learned from the outside world about seemingly important topics: oblivious transfer capacity, denoising, fountain capacity, and timing channels with jamming. All these can be studied also in the context of GTIT.

One can conceive of Information Theory in the broad sense as covering the theory of Gaining, Transferring, and Storing Information, where the first is usually called Statistics. For a somewhat different view the reader is advised to look at [61]. A broad class of statistical problems arises in the framework of hypothesis testing in the spirit of identification for different kinds of sources, with complete or partial side information or without it. Paper [37] is a start.

Information concepts play an important role in Game Theory. Information theorists usually think about choosing portfolios (see [60]), a direction started by J. Kelly ([83]), but there are many more connections which ought to be studied. We hint at them by listing basic papers [49], [50], [80], [104] and by pointing at the titles of the following survey articles [76], [88], [93] and [94] in the

Handbook of Game Theory. They contain the terms common knowledge, communication, correlated equilibria, search, and signalling.

We feel that animal communication ([58], [81]), psychology, and also neurology ought to be studied experimentally in the light of GTIT, with and without feedback.

A final question to Shannon's attorneys

The following last paragraph on page 376 is taken from "Two way communication channels", C. Shannon Collected Papers, 351–384.

"The inner bound also has an interesting interpretation. If we artificially limit the codes to those where the transmitted sequence at each terminal depends only on the message and not on the received sequences at that terminal, then the inner bound is indeed the capacity region. This results since in this case we have at each stage of the transmission (that is, given the index of the letter being transmitted) independence between the two next transmitted letters. It follows that the total vector change in equivocation is bounded by the sum of n vectors, each corresponding to an independent probability assignment. Details of this proofs are left to the reader. The independence required would also occur if the transmission and repetition points at each end were at different places with no direct cross communication."

According to our understanding the last sentence in this quote (which is put here in boldface) implies the solution of the capacity region problem for what is now called Interference Channel. Already in [5] we showed that the region obtained with independent sender's distributions is generally smaller than the capacity region.

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Award Announcements

2008 Claude E. Shannon Award

Prof. Bob Gray from Stanford was awarded the "2008 Claude E. Shannon Award." Prof. Gray will held his Shannon lecture at ISIT 2008 in Toronto, Canada.

2007 Information Theory Society Paper Award

The 2007 Information Theory Society Paper Award recognizes an exceptional publication in information theory, appearing in the period January 1, 2005 through December 31, 2006. At ISIT 2007 in Nice, it was announced that the award goes to:

"The Capacity Region of the Gaussian Multiple-Input Multiple-Output Broadcast Channel," by H. Weingarten, Y. Steinberg and S. Shamai (Shitz), which appeared in the IEEE Transactions on Information Theory, vol. 52, No. 9, pp. 3936-3964, September 2006.

This paper establishes the capacity region of one of the most important class of broadcast channels. In the process, new concepts and analytical tools are introduced. These results already impacted many other works in information theory.

A special mention should be given to the runner-up paper which was recognized by the award subcommittee to be an extremely strong contender:

"Mutual Information and Minimal Mean-Squared Error in Gaussian Channels", by D. Guo, S. Shamai (Shitz) and S. Verdu, IEEE Transactions on Information Theory, vol. 51, pp. 1261-1282, April 2005.

2007 Information Theory Society Aaron D. Wyner Distinguished Service Award

Dr. Jack Wolf, Stephen O. Rice Professor of Magnetics at the

Marc Fossorier

University of California at San Diego, has been awarded the 2007 Aaron D. Wyner Distinguished Service Award. The award honors individuals who have shown outstanding leadership in, and provided long standing exceptional service to, the Information Theory community.

2007 Information Theory Society Chapter of the Year Award

The award goes to the Seoul Chapter. The award recognizes the most active chapter during the previous year.

2007 Information Theory Student Paper Award

The first Information Theory Student Paper Award has been awarded to:

"Minimum Expected Distortion in Gaussian Layered Broadcast Coding with Successive Refinement," by Chris T.K. Ng, Deniz Gunduz, Andrea Goldsmith, and Elza Erkip

and

"Uplink Macro Diversity with Limited Backhaul Capacity," by Amichai Sanderovich, Oren Somekh, and Shlomo Shamai

Papers with a student author as the major contributor and presenter were eligible for this award. In total, 193 of the submissions to ISIT were self-marked as eligible for the student paper award. Of these, 106 were accepted for publication in ISIT and considered in the selection of the finalists. The complete list of the finalists is available at http://www.isit2007.org/index.php.

GOLOMB'S PUZZLE COLUMN™

EASY PROBABILITIES

- 1. Five of the ten decimal digits 0, 1, 2, 3, 4, 5, 6, 7, 8, 9 are selected at random, and arranged in ascending order as a < b < c < d < e. What is the probability that a + b + c > d + e?
- 2. You have n red marbles and n green marbles, with n > 1, which you will put into two jars in any way you like. A blindfolded contestant will select one of the two jars at random, and then select one marble from that jar at random. How should you distribute the 2n marbles into the two jars to maximize the probability that the selected marble will be green, and what is this maximized probability?
- 3. At the bridge table, when all 52 cards have been dealt, is it more likely that you and your partner together have all 13 hearts or none of the hearts?
- 4. You will play three tennis matches against two opponents, A and B, where A is a stronger player than B. You may choose to play them in either the sequence ABA or BAB.

Solomon W. Golomb

Which sequence gives you the better chance of winning two matches in a row?



- 5. The passenger next to you on the airplane (whom you never previously met) tells you she has two children. What is the probability that they are both girls if she says "yes" to:
 - (a) Is at least one of them a girl?
 - (b) Is the older one a girl?

(Here we assume that boys and girls are equally likely *a priori*, and that you have no information beyond the truthful answer to Question *a* or to Question *b*).

6. An opaque jar contains one marble, known to be either black or white (equally likely *a priori*). A white marble is now placed into the jar, which is shaken, and a marble is removed "at random" and observed to be white. What is the probability that the marble still in the jar is white?

Call for Nominations: International Dobrushin Prize

Grigory Kabatiansky and Michael Tsfasman, Institute for Information Transmission Problems and Independent University of Moscow

International Dobrushin Foundation

Roland L. Dobrushin (1929 - 1995) was an outstanding scientist of the 20th century. He is widely known for his achievements in information theory, probability theory, statistical physics, and mathematical linguistics. He was also a brilliant lecturer and research director, particularly well known for his support to young mathematicians. Dr. Dobrushin was one of the founders of the Independent University of Moscow. He created a laboratory at the Institute for Information Transmission Problems which now bears his name. The Dobrushin laboratory became known throughout the world for its staff of outstanding mathematicians including three Fields medal laureates.

Recently a Dobrushin Foundation was established by admirers of his talent. The purpose of the Foundation, which is funded by a private endowment, is to support science and scientists. Toward this goal, the Foundation launches the International Dobrushin prize, five Dobrushin scholarships for senior students of the Independent University of Moscow, and a Dobrushin grant for its professor.

International Dobrushin prize

The prize is awarded yearly to outstanding researchers for the totality of their work in the domains of research interests of Dr. Dobrushin, including information theory, statistical physics, probability theory, mathematical and computerlinguistics. The prize committee is formed of independent experts.

Nominations are accepted from any researcher, or a group of researchers, and must be sent before **May 10** to **dobrushinawards@yahoo.com** along with a list of significant publications of the candidate, a brief summary of the candidate's most important publications, and a list of three experts who have agreed to endorse the nomination.

The prize is awarded each year on June 20, Dr. Dobrushin's birthday. The winner receives a diploma, an equivalent of US\$3000, and is invited to present a lecture at the Institute for Information Transmission Problems in Moscow.

IEEE Seeking New Initiatives Proposals

The New Initiatives Committee (NIC) is now seeking proposals for IEEE New Initiatives as part of its two new programs: Rolling Submissions and Seed Grants. The NIC encourages wide dissemination of the program guidelines across the enterprise, and the NIC looks forward to receiving promising proposals. The committee will be meeting monthly, beginning in August, to review proposals. There is money available for the immediate funding of proposals approved during the balance of the 2007 fiscal year. Details of the new programs and the forms associated with them can be found on the IEEE New Initiatives web page located at http://www.ieee.org/web/aboutus/initiatives/index.html>.

There are two types of programs:

1) Rolling Submissions. The Rolling Submissions process (RSP) accepts proposals at any point in time with a decision to fund being rendered, in most instances, within 90 days of submission. Minimum funding requirement for RSP initiatives is US \$100,000 all of which should be expended during the first 12 months of the initiative. A brief project proposal form, which outlines the project, how it supports IEEE's strategic direction, estimated funding required and the project's goals and desired

outcomes, is required. If this short proposal is supported by the NIC, the project leader will be asked to develop a full project plan for approval by the NIC.

2) Seed Grants. The Seed Grant process (SGP) is designed to encourage any individual or group in the IEEE to innovate and be creative in the development of new programs, services, or activities that have the potential to move IEEE towards achieving its strategic objectives. Seed grants proposals may request up to US \$25,000. Decisions on Seed Grants are made by the NIC within 45 days, and funding is immediate. If approved, these projects must be completed within one year.

Completed proposals should be submitted by email to newinitiatives@ieee.org.

Questions regarding any aspect of the New Initiatives program should be directed to

Lew Terman (l.terman@ieee.org), John Keaton (j.c.keaton@ieee.org) or Matt Loeb (m.loeb@ieee.org).

IEEE Information Theory Society Board of Governors Meeting Baltimore, MD, USA, March 14, 2007

João Barros

Attendees: João Barros, Daniel Costello, Robert Calderbank, Anthony Ephremides, Elza Erkip, Andrea Goldsmith, Tor Helleseth, Ryuji Kohno, J. Nicholas Laneman, Steven W. McLaughlin, Muriel Médard, Prakash Narayan, David L. Neuho, Vincent Poor, Bixio Rimoldi, Anant Sahai, Sergio D. Servetto. The meeting was called to order at 18:14 by Society President Bixio Rimoldi, who welcomed the members of the Board.

- 1. The agenda was approved and distributed. Board members were also encouraged to look at the agenda and other materials online at the new Society development server.
- The Board unanimously approved the minutes of the previous meeting (Allerton House, Monticello, Il, USA, September 27, 2006).
- 3. The Board unanimously approved the following amendment to the previous Minutes (Puntadel Este, Uruguay, March 14, 2006): "The Board was reminded that the IT society has been moved to Division X." should read "The Board was reminded that the IT society has been moved to Division IX."
- 4. The President thanked previous past presidents for their dedication and leadership, as well as their support in the recent transition. The President presented his report and miscellaneous announcements.

The President reported on the state of the Society, including the IT Transactions, conferences and workshops, status of various initiatives, and membership.

The President reported on the status of the quinquennial IEEE Review of the IT Society.

The Board discussed the five-page limit to correspondence items in the IT Transactions. The President reported some uneasyness from the officers about this decision and whether or not it should be reconsidered, given that the growth of the Transactions has stopped and that the policy leaves room for interpretation: At this point it is up to an associate editor to decide what to do with a correspondence item of high quality that exceeds the five-page limit. Anthony Ephremides commented that the Transactions should have a single category for all papers. The consensus was that a decision has been made and that sometime (e.g. a year) should pass before reconsidering this issue.

The Board discussed the new initiatives under consideration for 2007. Muriel Médard will co-ordinate an outreach effort of the IT Society directed towards undergraduates and possibly high-school students.

5. Daniel J. Costello presented the Conference Coordinator's report on the current status of symposia and workshops. The individual reports for each event are available online.

The Board unanimously approved the technical co-sponsorship and inclusion in IEEE Xplore for NETCOD 2008. David Neuhoff reported on a Memorandum of Understanding regarding technical co-sponsorship and IEEE Xplore inclusion.

- 6. Steven W. McLaughlin explained the process of appointing the Editor in Chief. The Board unanimously approved the appointment of Ezio Biglieri as Editor in Chief of the IT Transactions.
- 7. Ryuji Kohno presented a proposal to link and publish abstract of ISITA's papers in IEEE Xplore. The conference committee will evaluate this proposal and produce a recommendation.
- 8. David Neuhoff reported on the ongoing revision of the IT Society's bylaws. The Board unanimously approved the proposed changes to the Constitution. The Board unanimously approved the proposed ammendments to the Bylaws.
- 9. Vincent Poor presented the Editor and Chief's report and proposed four new associate editor appointments. The Board approved the following appointments for Associate Editor (AE) of the IEEE Transactions:
 - Adam Krzyzak for Pattern Recognition, Statistical Learning and Inference;
 - Urbashi Mitra for AE At-Large;
 - Helmut Bölsckei for Detection and Estimation;
 - Hirosuke Yamamoto for Shannon Theory.

The page budget has been met approximately. A hierarchical table of content has been introduced. The IT Transactions passed the five-year review by the IEEE easily.

- 10. Andrea Goldsmith presented the Student Committee report. The events organized by the Student Committee have had very strong attendance records. Sergio D. Servetto was appointed as the new co-ordinator for this initiative.
- 11. Anant Sahai presented the Treasurer's report. The Society's finances were reviewed and found to be healthy. The financial activities of the Society conferences and workshops were reported in the Treasurer's report online. The Board discussed several options for using the available surplus funds.
- 12. J. Nicholas Laneman presented the Online Editor's report. There was a motion to approve an ad-hoc committee on online content and services. The Board unanimously approved the motion.
- 13. There was no new business.
- 14. The next Board meeting will be held at ISIT in Nice.

The meeting was adjourned at 23:33.

Call for Participation, ICIAfS/IVRI 2007, Melbourne, Australia, December 3-6 2007

Third International Conference on Information and Automation for Sustainability ICIAfS 2007 with Second Intelligent Vehicles and Road Infrastructure Conference - IVRI 07 and Third International Conference on Intelligent Sensors, Sensor Networks and Information Processing ISSNIP 07 3-6 December 2007, Melbourne, Australia.

Conference website: http://www.issnip.org/2007/coconf.html.

Topics:

The scope of the conference will include, but is not limited to the following four themes:

Theme 1: Safety and Security: Operator fatigue, automated explosive detection, demining, intrusion detection, collision warning, collision avoidance, human factors, etc Sub-Theme: Road: lane guidance, driver status monitoring, transport protocols, automated platooning of commercial vehicles, etc.

Theme 2: Efficiency, Energy and the Environment: Engine emissions, alternative fuels, engine modeling and simulation, hybrid vehicles, fuel cells, fuel consumption, optimization of engine design, etc.

Theme 3: Sensors and Telematics: Route guidance, GPS applications, powertrain control, vehicle stability control, sensor networks, sensor design, signal processing, data fusion, vehicle tracking and identification etc.

Theme 4: Automation: Mechatronics, robotics, intelligent manu-

facturing, etc.

Conference proceedings: As in 2006 conference, the proceedings will be available as a CD and indexed in IEEE Xplore.

Sponsors:

The Society of Automotive Engineers (SAE) Australasia, ARC Research Network on Intelligent Sensors, Sensor Networks and Information Processing (ISSNIP), and The University of Melbourne are proud to extend an invitation to the two conferences ICIAS and IVRI in 2007. Both conferences expand upon their themes of their previous conferences.

Technical Co-sponsorship will be sought from IEEE Region 10 and relevant IEEE Societies.

Important dates:

Conference dates: December 3-6, 2007 Notification of acceptance: August 14, 2007

Submission Deadline: July 31, 2007 (Special Sessions: Aug. 31)

Camera ready manuscript: October 1, 2007

Conference Secretariat:

SAE-Australia Tel: +61 3 9326 7166 Fax: +61 3 9326 7244

Email: harrycw@unimelb.edu.au



Editorial

Ezio Biglieri (e.biglieri@ieee.org), Editor-in-Chief, IEEE Transactions on Information Theory

"One of the Editor's few perquisites is the prerogative of publishing his own opinions from time to time, uninvited." [1]

"You must remember this..."

Regrettably, it is not an established tradition that the incoming EiC of our Transactions addresses their readers with an Editorial, rexamines the past of the publication, directs attention to its weak points, and announces novelties. And yet, whenever they were published, the few editorials of our past provided us with a sharp overview of the discipline and its evolution, as seen from the vantage point of the flagship publication in the field. The two examples that follow prove eloquently this point. Read, for instance, what it was said about Information Theory back in 1959. I cite without comments from [2]:

As befits the role of an American mathematician in modern society, I have nothing practical to say about information theory. However the devotees of this theory may be interested in the reactions of an outsider who has followed some of its development. In spite of all the suggestive work by Wiener, Shannon, and their successors, the main thing that strikes an outsider is that there are so few theoretical results. In fact almost every time a writer proves an assertion connecting the capacity of a channel with the entropy of a source, his paper P_n is succeeded by a paper P_{n+1} which, instead of generalizing or extending the results of P_n , is devoted to pointing out and correcting some defect or insufficiency in it. The paper P_{n+1} , in its turn, receives the same harsh treatment, and so on. Moreover, in this presumably convergent process of purging and purifying, the theorems become more and more attenuated and inapplicable as their hypotheses become more restrictive. Even more extraordinary is the fact that this process of organizing what seems to be the very basis of the subject seems to have no effect whatever on its applications! Can it be that the existence of a mathematical basis is irrelevant, and that the basic principle is the very idea that there is a context in which the word "information" is accepted by general agreement and used in an intuitive way, and that no more is needed?

A more recently Editorial, written by the then EiC Dave Forney, set a tone and made predictions on whose validity one can still (at least in part) agree: [1]

[Information Theory], as an increasingly mature field, it is not exempt (if it ever was) from the laws that govern the evolution of all sciences. New and basic ideas are always rare. The research frontier becomes ever more esoteric. Much work is done that does not speak to today's real needs, or the future's. Yet work proceeds that will have the cumulative effect over the course of time of completely changing the outlines of the field, its practice, and our understanding of it. Which work falls in which category is not always immediately clear. Without great daring, one can make a few predictions, valid now or any time.

1) The field will not die, but it will change. It has the good fortune after all to be an engineering field, linked to technologies that are expanding with great vigor, and that yearly make feasible and economic ever more sophisticated kinds of information processing. It also has an

intellectual beauty that will continue to attract some of the very best students.

- 2) Ten years from now the subjects of papers in this TRANSACTIONS will be largely different from (and more abstruse than) today's; today's contributors will be complaining that the TRANSACTIONS has become unintelligible and irrelevant.
- 3) Twenty-five years from now the present will be seen as a rather ignorant and uninformed time, full of misguided, naive, and trivial work; yet at the same time our successors will perceive in this era the laying of the foundations for the "information theory" of that day, and will envy us for working at a time when so much was fresh and new.

"As time goes by"

Our Transactions started in 1954. The first EIC, then known as Chair of the Publications Committee, was L. G. Fischer (until 1958); G. A. Deschamps followed in the same position until 1960. Meanwhile, these two were overlapped by R. M. Fano who headed the "Editorial Review" from 1957 to 1961. In chronological order, they are [3]: A. Kohlenberg, D. Van Meter, Carl Helstrom, Dave Forney, Jim Massey, Neil Sloane, Bob Gray, Aaron Wyner, Toby Berger, Bruce Hajek, Dick Blahut, Rob Calderbank, Alex Vardy, Paul Siegel, and Vince Poor.

All my predecessors were highly successful in maintaining and enhancing the reputation for high standards that our journal enjoys. As a recent proof of this, Vince Poor, during the IT Society Board of Governors meeting in Nice, June 2007, reported that the Transactions underwent their five-year review on February 15, 2007, at the IEEE TAB meeting series in Los Angeles. The principal findings in the final report of the review committee read: "The IEEE Transactions on Information Theory is an exemplary periodical among all IEEE publications, with a very strong tradition in quality. The impact factor is among the highest of all IEEE periodicals, and has been for several years. The Editorial staff is a dedicated group of volunteers who are all focused on the single goal of maintaining the highest standards of the Transactions. While past problems with respect to timeliness have marred this exemplary performance, over the last five years since the last review the Information Theory Society has worked to steadily reduce the submission-to-publication time to the point now that it is within target guidelines for IEEE Periodicals. (...) We recommend that the Information Theory Society stay the course and continue to improve on your already outstanding periodical." In addition, a recent analysis of journal status, combining popularity and prestige of scholarly publications, has ranked our Transactions as the top "Prestigious Journal" in Computer Science. This article is posted on ArXiv at http://www.arxiv.org/PS_cache/cs/pdf/0601/0601030v1.pdf

"It's still the same old story"

I cannot conceal the fact that one of the main problems with these Transactions (as in general with scholarly publishing based on peer reviews) has been the long time elapsing between submission and publication. This causes dissatisfaction among authors (who want their results to be made quickly available to our com-

munity) as well as among readers (who want to be informed of results well before the end of their shelf life). I plan to devote much attention to this problem, and do my best to contribute to its solution, (a) prompting Associate Editors and Reviewers to be punctual (although not at the price of decreasing the quality of the reviews and of the publication decisions), and (b) by trying new ways to enrich the reviewing process (see below). My goal will be to shorten the publication time well within IEEE recommendations (50% of submissions to receive their first decision within 90 days from submission, and 80% of them to have a publication time shorter than 1 year).

"What the future brings"

Open reviewing [4]: On an experimental basis, we plan to allow open reviewing of submissions. The procedure will be the following: If a paper is posted in arXiv, with the explicit indication "Submitted to the IEEE Transactions on Information Theory," then its readers are allowed to send the EiC their comments about it. After verifying that these are not frivolous or obviously biased, the EiC forwards them to the Associate Editor in charge of the paper to supplement regular peer reviews.

Invited papers: I intend to continue the policy of publishing invited tutorial/state-of-the-art papers on a regular basis. It has been about 10 years after the publication of an entire issue of the Transactions devoted to papers summarizing the first 50 years of Information Theory. Since then, several exciting new areas have been developed. My plan is to publish a series of invited papers on the areas that were not covered in that issue, and on areas where a large body of new results was developed. Whenever possible, these papers should be written by teams of authors exhibiting a maximum of diversity in their approaches to the discipline.

The readers of the Transactions are urged to recommend topics in which they would like to see such papers.

A final note on style: Our mission as scientists includes not only the advancement of science, but also the communication of its progress to our community. In this process, the clarity of scientific writing plays a central role: this basically consists of saying what one really means, rather than hint at it through delphic academic utterances left to the reverential exegesis of admiring disciples. (Some papers make me remember Iamblichus' statement about Pythagoras and the Pythagoreans: "Their writings and all the books which they published were not composed in a popular and vulgar diction, but in such a way as to conceal, after an arcane mode, divine mysteries from the uninitiated.") Arguments should be presented in the most orderly and logical manner, with close attention paid to how one's facts are marshaled. In addition, authors should be aware of the fact that making notations harder does not make paper feel more scientific. Better style means improved legibility, and, eventually, a better service rendered to our community. I intend to have more attention paid to the quality of the IT Transactions writing style.

References

- [1] G. D. Forney, Jr., "Editorial," IEEE Trans. Inform. Theory, Vol. IT-19, No. 1, p. 2, January 1973.
- [2] J. L. Doob, "Editorial," IEEE Trans. Inform. Theory, Vol. IT-5, No. 1, p. 3, March 1959.
- [3] A. Ephremides, Private communication.
- [4] Based on a suggestion of Prakash Narayan.

Letters to the Editor

I inaugurate here, with the reply to my first Letter to the Editor, a more personal space to exchange opinions and reflections about this newsletter and other topics relevant to our society. I will do my best to adequately answer your letters. Thanks in advance for contributing in making the newsletter a more valuable and interactive space.

Dear Editor:

As one of the organizers of 1983 ISIT in St Jovite, Quebec and of the 1995 ISIT in Whistler I was overwhelmed with nostalgia after reading about them in Tony Ephremides' June 2007 Historian Column. As an immigrant to Canada, I appreciated very much Tony's remarks about this magnificent country.

Next year will be the 25th anniversary of the 1983 ISIT which was cochaired by Ian Blake and John Anderson. St Jovite has now merged with the municipality of Mont-Tremblant. The resort where the Symposium took place-Auberge Gray Rocks, by the shores of Lac Ouimet-is still there (www.grayrocks.com). I plan to organize a mini reunion of those who wish to come (please send me an e-mail to vijayb@ece.ubc.ca if you are interested) immediately following ISIT 2008 in Toronto. As Tony said, "it was only like yesterday!"

Sincerely,

Vijay Bhargava University of British Columbia Vancouver, Canada

Dear Dr. Vijay Bhargav:

I sincerely join you in expressing my fondness of Tony's warm and captivating writing style. Thanks Tony for your great historian columns!

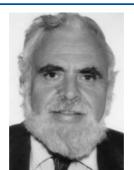
The idea of organizing a reunion to celebrate the 1983 ISIT jubilee anniversary in Whistle is commendable. One (among the many) special and distinctive characteristics of our society is the friendship among its members. This makes our technical events remarkable beyond the high quality of presented works.

I trust the reunion will be a success and invite you to tell us about it next year with a letter or a report.

GOLOMB'S PUZZLE COLUMN™

CONNECT THE DOTS

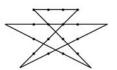
Solomon W. Golomb



1. The four 6-segment circuits on the 4×4 array of dots are:

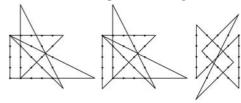




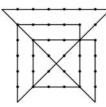




2. Here are three inequivalent 8-segment circuits on the 5×5 array of dots.



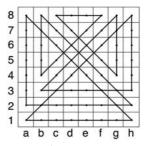
3. Here are two 10-segment circuits on the 6×6 array of dots.



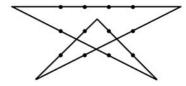


The solution on the right stays within the convex hull of the 6×6 array of dots.

4. This 14-move queen's tour of the chessboard was first published by Sam Loyd. It is included in *Sam Loyd and His Chess Problems*, compiled by Alain C. White, published 1913 by Whitehead and Miller; Dover reprint, 1962. The queen's circuit is: a1-h1-a8-a2-h2-b8-b4-f8-c8-g4-g8-b3-h3-h8-a1.



5. Here is the unique 5-segment circuit on the 3×4 array of dots.



Reference. The definitive article on this subject is by S.W. Golomb and J.L. Selfridge, "Unicursal Polygonal Paths and Other Graphs on Point Lattices," Pi Mu Epsilon Journal, Fall, 1970.

News From the Communications Program at NSF

by Sirin Tekinay, Program Director



Dear reader,

This is the eighth column in this series- by the time it appears in print and online, I will have started my third year at the NSF. My appointment as your program officer in Washington ended up getting extended another year. I look forward to this space serving its purpose of fueling our interaction on ideas, visions, and issues that impact us all as professionals in the communications community as I write about relevant NSF programs and news.

New and Upcoming Solicitations

I am delighted to report that I will serve as the chair of the NSF-wide Cyber Enabled Discovery and Innovation Implementation Team (CDIIT). I had reported on the Science of Interaction write up that led to CDI funding earlier [1]. As the chair of the NSF-CDIIT, I will be able to report to you the bigger picture of this exciting new program that includes research in information theory, communication theory, network theory, signal processing, and complexity, to name a few. Our first deadline is to draft the NSF-solicitation is September 30. I recently called the kickoff meeting for this five year, \$750M program. Our charter is to come up with the most comprehensive solicitation possible, so as not to deviate significantly from it in the years to come.

I'm also happy to report that I have been leading the authoring of the new directorate-wide research program solicitation that aims to bring together all relevant activities towards the clean slate Internet vision. Network theory, which we had accommodated in Theoretical Foundations (as Science for Internet's Next Generation; SING) until this year, will be included in this new wider-scope CISE program. We hope to stimulate lots of teaming; in particular collaborations across the many communities traditionally served by the different divisions in our directorate. The planned posting date of the solicitation is late this year.

I continue to serve as the representative of our directorate on the Interdisciplinary Graduate Education Research Traineeship (IGERT) program coordination committee. At the time of writing, we are working on formulating the IGERT 2008 program solicitation, which is an upgraded version with frequently asked questions answered and new review criteria added.

Review criteria listed in solicitations are meant to not only guide proposal writing, but also reviewers (panelists and ad hoc reviewers alike) in filing their reports on the proposals. The two sets of contributors to NSF's mission, the proposers and reviewers, are given the exact same list, which is transparent to all.

News on Communications Research

Theoretical Foundations 2007 competition is about to be concluded: most of the declinations have been sent out, and we are distributing the available funds among the prioritized proposals. As a result, communications and network theory related proposals

will receive a combined total of \$10M, all of which will be spent in the form of "standard grants." Standard grants, as opposed to continuing grant increments, are those where the total funds for a multi-year project are allocated from the current year's budget. I am proud to have been able to sustain a twenty per cent success rate in our program without mortgaging the future of the program by committing continuing grant increments from future years' unknown funds. It was a hard decision to decline the last few proposals; however, despite the bitter medicine we took to ensure the future financial health of the program, I was still able to translate the slight increase in the program budget into a modest increase in the success rate.

We will run the TF08 competition with a calendar similar to this year's. This means we are gearing up to formulate and post the solicitation mid-fall. A couple of changes you can expect are the following: a researcher can have their name on up to two proposals as opposed to one; and SING will not be an area of emphasis within TF. Rather, it will take its place in the directorate-wide research portfolio, whose solicitation is also on the drawing boards.

We just received our CAREER proposals. At this time, they are going through the NSF compliance check. At a first glance, the statistics seem consistent with past years.

On a Personal Note

Your program officer received the NSF Director's Award for Program Management Excellence. The citation reads: "in recognition of her superior management and planning in the Division of Computing and Communication Foundations, her proactive development of new areas of research and education, and her active promotion of teamwork at all levels of the organization." The secret is that I never feel I am doing a superior job. Our greater community deserves the best representation and service possible, which is an endless task I feel humbled to work on. So I received the award in the name of all of us. Thank you.

In preparation for my return to my home institution, I'm grateful that I was given the opportunity to participate in the Summer Institute for Higher Education Resource Services [2]. I learned a universe of knowledge on administration in the academe, while networking with brilliant academic leaders from many different backgrounds. I am convinced that good leadership in administration is every bit as educational as teaching in the classroom.

NSF People

In every column, I introduce some of the people I work with; who embody the culture and spirit of NSF. This time, with deepest sorrow I remember my dear colleague and friend, Dr. Stephen Mahaney, who passed away on June 26, Tuesday, after a very sudden illness. Steve was a Senior Advisor in CISE. He is survived by his wife Jean-Marie, and two daughters, Kylen and Kate. Steve

helped shape the Computing Research Infrastructure program, managed several center-scale activities, and carried too many other responsibilities to list. Steve was my lunch buddy, mentor, and go-to person with all kinds of questions. His sense of humor was unparalleled. He taught me how you can tell an "outgoing" engineer; he/she is the one that looks at the other person's shoes during a conversation as opposed to their own. I miss him dearly, we all do. So long, Steve...

The "Social Scene"

On June 19, Tuesday, following the Director's Awards Ceremony, we had a big celebration in the atrium of the beautiful NSF building. As an award winner, I would have liked to enjoy the congratulations in the name of our program and community; however, I had to run back to the IGERT panel I had abandoned for a couple of hours. Being at two places at one time is still an open research area.

Shortly after that, I left for Bryn Mawr, PA, where the HERS Summer Institute was held. The next time I was able to get together with a group of NSF colleagues was to honor and celebrate Steve's life. It turns out, Steve and I shared our birthday, which was

the day after his wake. So we celebrated my birthday and his...

This column was written mostly on the beautiful Bryn Mawr campus, after hours.

... Till next time, dream big, and keep in touch!

Sirin Tekinay
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http://www.nsf.gov/staff/staff_bio.jsp?lan=stekinay&org=CCF

REFERENCES:

&from=staff

[1] http://www.nsf.gov/about/budget/fy2008/pdf/39-fy2008.pdf

[2] http://www.hersnet.org

Call for Proposals for the Banff International Research Station 2009

Bob Gray, Stanford University

Below is a formal call for proposals for 2009 workshops at the Banff International Research Station (BIRS) in the Canadian Rockies. BIRS hosts 5 day and 2 day workshops in mathematics of up to 42 participants and provides lodging and (excellent) food. In recent years BIRS has been expanding into the mathematical side of engineering. I encourage the Information Theory community to consider this excellent opportunity to do intensive cooperative research in one of the world's most gorgeous locations. Check out the Website below (or see my own Websites for the two workshops I have been involved with for photos, http://ee.stanford.edu/~gray/birs/ and http://birs07.stanford.edu/). Proposals are due soon, 1 October 2007.

The Banff International Research Station for Mathematical Innovation and Discovery (BIRS) is now accepting proposals for its 2009 programme. The Station provides an environment for creative interaction and the exchange of ideas, knowledge, and methods within the mathematical, statistical, and computing sciences, and with related disciplines and industrial sectors.

Full information, guidelines, and online forms are available at the website http://www.birs.ca/. Proposal submissions should be made using the online submission form at https://www.birs.ca/proposals/.



2008 IEEE International Symposium on Information Theory

Toronto, Canada, July 6–11, 2008

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The 2008 IEEE International Symposium on Information Theory (ISIT 2008) will be held from Sunday, July 6th, to Friday, July 11th, 2008, at the Sheraton Centre Toronto Hotel, in Toronto, Ontario, Canada. Toronto is Canada's largest city, and is directly accessible by air from major cities around the world. The symposium hotel is in the city centre, conveniently located near shopping, museums, and public transportation.



Previously unpublished contributions from a broad range of topics in information theory are solicited, including (but not limited to) the following areas:

> Coding theory and practice Communication theory Compression Cryptography and data security **Detection and estimation** Information theory and statistics Information theory in networks

Multi-terminal information theory Pattern recognition and learning Quantum information theory Sequences and complexity Shannon theory Signal processing Source coding

In addition to submitting new results in the above areas, researchers in related fields and researchers working on novel applications of information theory are encouraged to submit contributions. The paper submission deadline is January 7, 2008, with notification of acceptance by March 31, 2008.

Detailed information on paper submission, technical program, accommodation, tutorials, travel, and excursions will be posted on the symposium web site: http://www.isit2008.org.

For general inquiries, please contact one of the symposium co-chairmen:

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First Call For Papers Third International Symposium on Communications, Control and **Signal Processing**

Le Méridien Hotel, St. Julians, Malta March 12 - 14, 2008

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The 3rd International Symposium on Communications, Control and Signal Processing (ISCCSP'08) will be he ld at the Le Méridien Hotel, St. Julians, Malta. Its purpose is to be a forum for technical exchange amongst scientists having interests in Communications, Control and Signal Processing. The technical program will include plenary lectures, regular technical sessions, and special sessions covering the three major tracks.

Malta is at the centre of the Mediterranean and is well known for its hospitality. The rich archeological and cultural heritage dating back several millennia provide an interesting backdrop to the Symposium.

Prospective authors are invited to submit full-length, four page papers in portable document format (PDF) to the ISCCSP Technical Committee. All papers will be handled and reviewed electronically.

For up-to-date information and paper submission, please visit the Symposium web site: http://www.eng.um.edu.mt/isccsp2008. Proceedings of the Symposium will be published and provided to attendees on CD-ROM. Please note that, at least one full paying author of each accepted paper must register for the Symposium before the indicated deadline.

SCHEDULE FOR AUTHORS

Deadline for submission of papers October 1, 2007 Notification of acceptance December 9, 2007 Deadline for submission of camera-ready paper January 15, 2008 Deadline for author registration January 20, 2008

Driss Aboutajdine, Morocco Sergio Benedetto, Italy Paul Dan Cristea, Romania Edmond Jonckheere, U.S.A. S-Y Kung, U.S.A. Sanjoy Mitter, U.S.A. Umapathy Reddy, India

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ITW 2008 PORTO

IEEE Information Theory Workshop | May 5-9, 2008 | Porto, Portugal

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The 2008 IEEE Information Theory Workshop (ITW 2008) will take place on May 5-9 in Porto, Portugal. The chosen venue is the magnificient Palacio da Bolsa, right by the River Douro, in the heart of the World Heritage Site of Porto.

Invited sessions will take a brief look into the recent information theory past to commemorate the 60th anniversary of Shannon's landmark paper, and then proceed to explore opportunities for information theory research in quantum computation, biology, statistics, and computer science. A large majority of papers will be contributed, and are solicited in (but not limited to) the following areas:

- Coding theory and practice
- Communication theory
- Compression
- · Cryptography and data security
- · Detection and estimation
- Information theory and statistics
- · Information theory in networks
- · Multi-terminal information theory
- Pattern recognition and learning
- Quantum information theory
- · Sequences and complexity
- · Shannon theory
- · Signal processing
- Source Coding



Contributions by authors new to the information theory community are particularly encouraged. Abstracts of up to 5 pages should be submitted by **November 16, 2007** following the guidelines on the workshop web page. Authors will be notified of acceptance decisions by **February 16, 2008**. The final version, to be published in the workshop proceedings, will be due by **March 7, 2008**.

Information regarding the technical and social programs, final manuscript format, workshop registration, and hotel accommodations will be posted on the workshop website at:

http://www.dcc.fc.up.pt/~itw2008/

Conference Calendar —

DATE	CONFERENCE	LOCATION	CONTACT/INFORMATION	DUE DATE
August 29-30, 2007	12th International OFDM- Workshop 2007 (InOWo'07)	Hamburg, Germany	http://ofdm.tu-harburg.de	April 13, 2007
Sept. 2-6, 2007	2007 IEEE Information Theory Workshop (ITW 2007)	Lake Tahoe, CA, USA	http://www.ece.tamu.edu/itw2007/	April 1, 2007
Sept. 26-28 2007	The Annual Allerton Conference on Communication, Control and Computing (Allerton 2007)	Monticello, IL, USA	http://www.comm.csl.uiuc.edu/allerton/	July 1, 2007
Oct. 1-3, 2007	2007 IEEE 65th Vehicular Technology Conference VTC2007 (VTC 2007 Fall)	Baltimore, MD, USA	http://www.ieeevtc.org/ vtc2007fall/index.php	Feb. 10, 2007
Nov. 4-7 2007	The Asilomar Conference on Signals, Systems, and Computers (Asilomar 2007)	Monterey, CA, USA	http://www.asilomarssc.org/	June 1, 2007
Nov. 26-30, 2007	2007 IEEE Global Communications Conference (GLOBECOM 2007)	Washington D.C., USA	http://www.comsoc.org/ confs/globecom/2007/	March 15, 2007
Jan. 3-4, 2008	4th Workshop on Network Coding, Theory and Applications (NETCOD2008)	Hong Kong	http://netcod2008.ie.cuhk.edu.hk	September 1st, 2007
Jan. 14-16, 2008	7th International ITG Conference on Source and Channel Coding (SCC 08)	Ulm, Germany	http://www.mk.tu-berlin.de/scc08	July 21, 2007
January 28 - February 1, 2008	2008 Information Theory and Applications Workshop (ITA 2008)	San Diego, CA, USA	http://ita.ucsd.edu/workshop.php	TBA
March 12-14, 2008	The 2008 International Zurich Seminal on Communications (IZS 2008)	r Zurich, Switzerland	http://www.izs2008.ethz.ch	October 8, 2007
March 12-14, 2008	3rd International Symposium on Communications, Control and Signal Processing (ISCCSP08)	St. Julian, Malta	http://guinevere.eng.um.edu.mt/isccsp2008/	October 1, 2007
May 5-9, 2008	2008 IEEE Information Theory Workshop (ITW 2008)	Porto, Portugal	http://www.dcc.fc.up.pt/~itw2008/	March 7, 2008
July 6 – 11, 2008	2008 IEEE International Symposium on Information Theory (ISIT 2008)	Toronto, Canada	http://www.isit2008.org	January 7, 2008